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Title: Fundamental symmetry tests in the lepton sector

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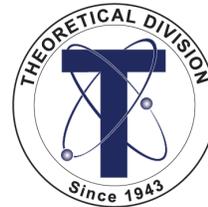
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Fundamental symmetry tests in the lepton sector

Kaori Fuyuto

Los Alamos National Laboratory



W. Dekens, J. de Vries, KF, E. Mereghetti, G. Zhou
JHEP06(2020)097

V. Cirigliano, KF, C. Lee, E. Mereghetti, B. Yan
JHEP03(2021)256

December 1, 2021
University of Arizona

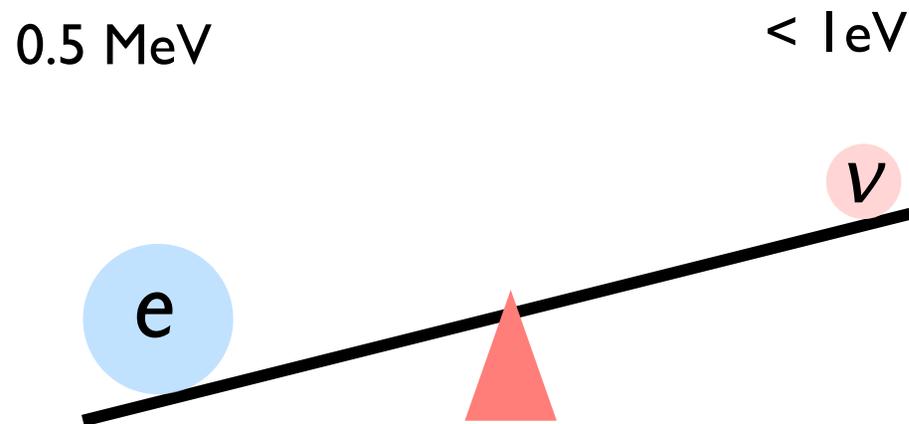
Outline :

1. Introduction
2. Neutrinoless double beta decay
 - EFT approach with light sterile neutrino
 - Application to leptoquark model
3. LFV Tau to e transition
 - EIC vs other experiments
4. Summary

Introduction

Neutrino mass

The observation of neutrino oscillation confirms neutrinos have mass.



Open question :

What is the origin of the tiny but non-vanishing masses of the neutrinos?

Neutrino mass



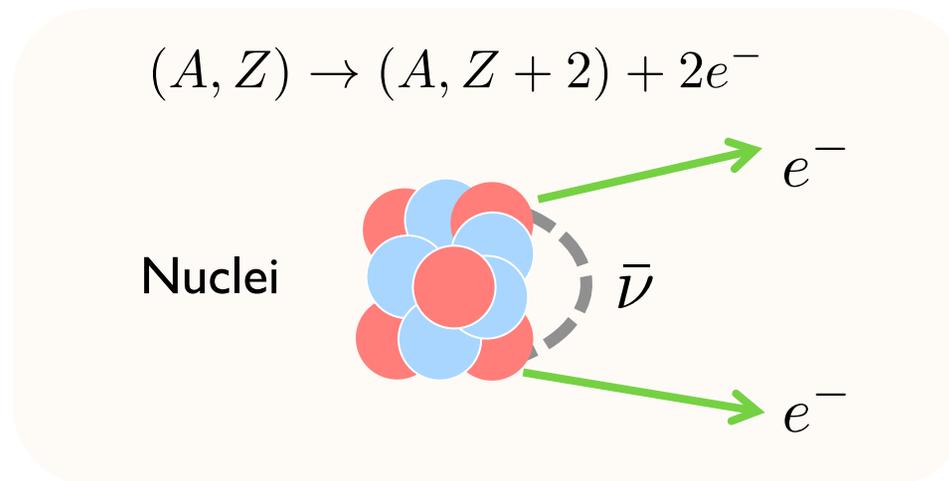
Key approach : Fundamental symmetry tests

- * Search for violation of symmetry which is preserved in the Standard Model

Neutrino mass

★ Key approach : Fundamental symmetry tests

I) Lepton number violation



* This process violates lepton number by two units.

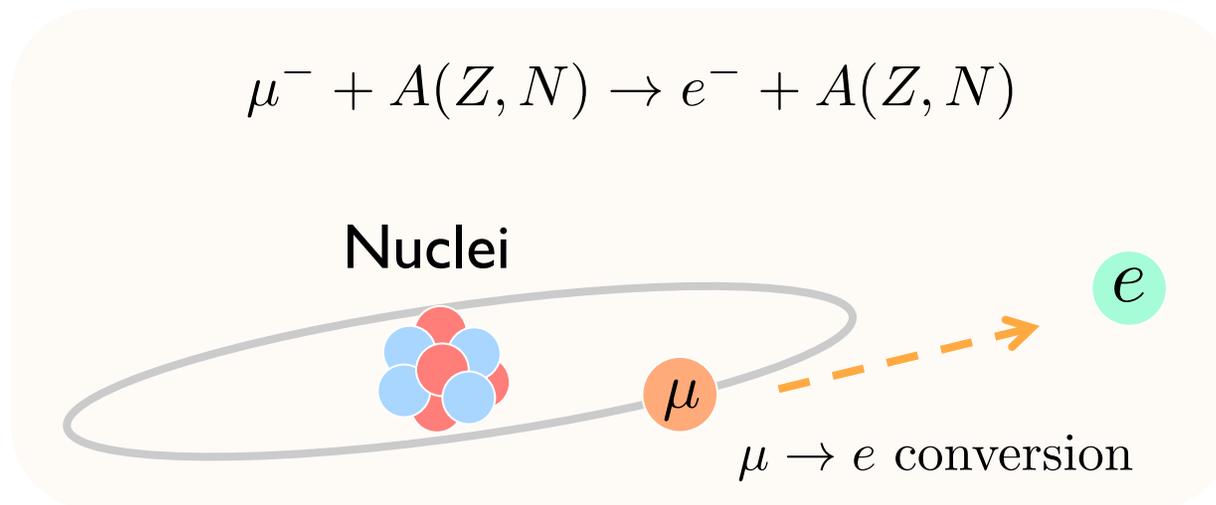
Neutrino mass



Key approach : Fundamental symmetry tests

- 1) Lepton number violation
- 2) Charged-lepton flavor violation

Ex) $\mu \rightarrow e\gamma$, $\mu \rightarrow e$ conversion, $\tau \rightarrow e\gamma \dots$



Neutrino mass



Key approach : Fundamental symmetry tests

- 1) Lepton number violation
- 2) Charged-lepton flavor violation

Ex) $\mu \rightarrow e\gamma$, $\mu \rightarrow e$ conversion, $\tau \rightarrow e\gamma \dots$

Why important?

Various hypotheses, i.e., New Physics, to explain nonzero neutrino mass predict the violation.

* Neutrinoless double beta decay and Tau to e LFV

Today

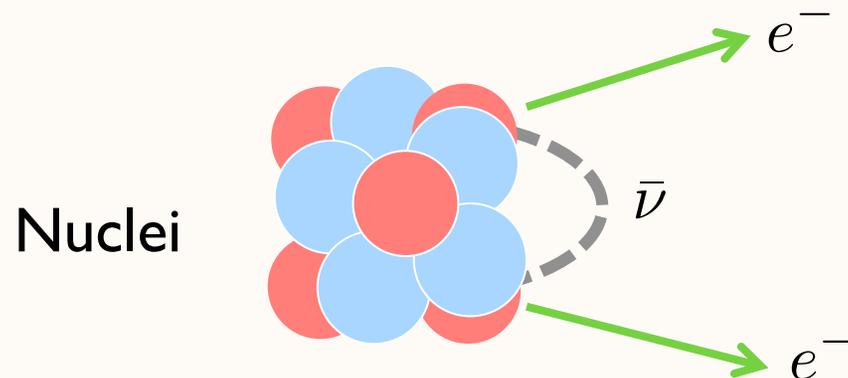


Neutrinoless double beta decay

Neutrinoless double beta decay

Double β decay without neutrino emission

$$(A, Z) \rightarrow (A, Z + 2) + 2e^{-}$$



The process can occur if neutrino is a *Majorana* particle.

Majorana mass

Right-handed neutrino : ν_R

~ Gauge singlet (Sterile neutrino)

$$\mathcal{L}_{\nu_R} = \overset{\text{Yukawa}}{-Y_\nu \bar{L} \tilde{H} \nu_R} - \overset{\text{Majorana Mass}}{\frac{1}{2} \overline{\nu_R^c} M_R \nu_R} + \text{H.C}$$

Majorana mass

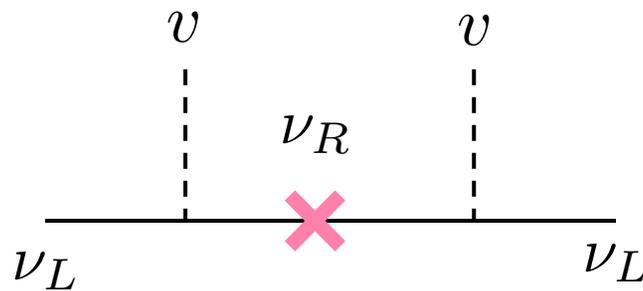
Right-handed neutrino : ν_R

~ Gauge singlet (Sterile neutrino)

Yukawa

Majorana Mass

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$



✗ : Mass insertion

v : Higgs VEV

Majorana mass

Right-handed neutrino : ν_R

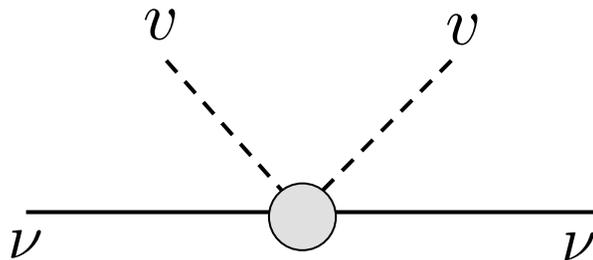
~ Gauge singlet (Sterile neutrino)

Yukawa

Majorana Mass

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \bar{\nu}_R^c M_R \nu_R + \text{H.C}$$

Majorana mass term is induced.



$$\mathcal{L}_{\text{mass}} = -\frac{1}{2} \bar{\nu} m_\nu \nu$$

$(\nu = \nu^c)$

Majorana mass

Right-handed neutrino : ν_R

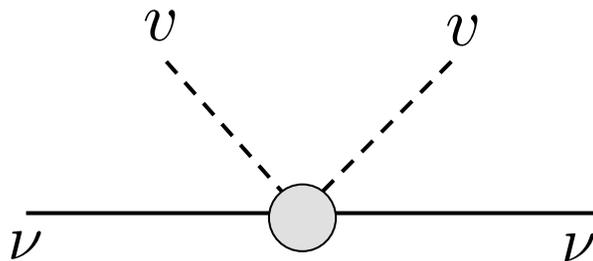
~ Gauge singlet (Sterile neutrino)

Yukawa

Majorana Mass

$$\mathcal{L}_{\nu_R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$

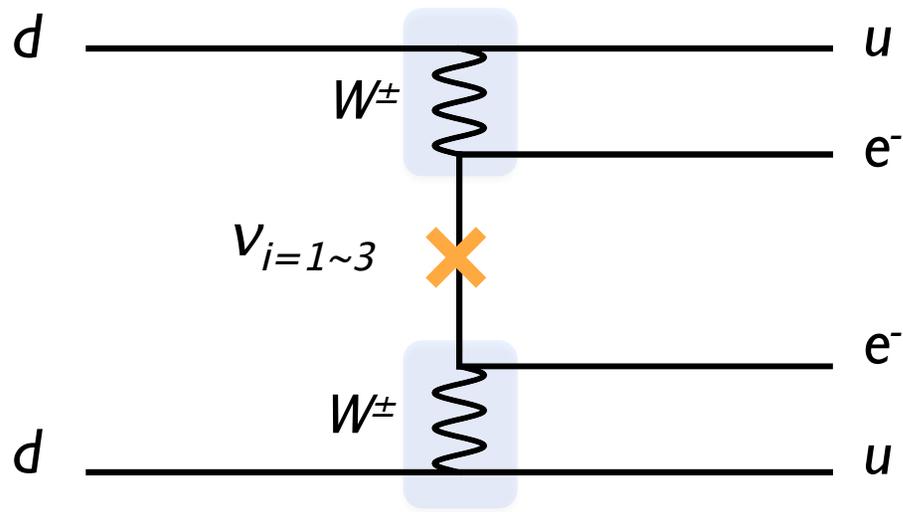
If M_R is much heavier than EW scale,



$$m_\nu \sim \frac{Y_\nu^2 v^2}{M_R}$$

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$



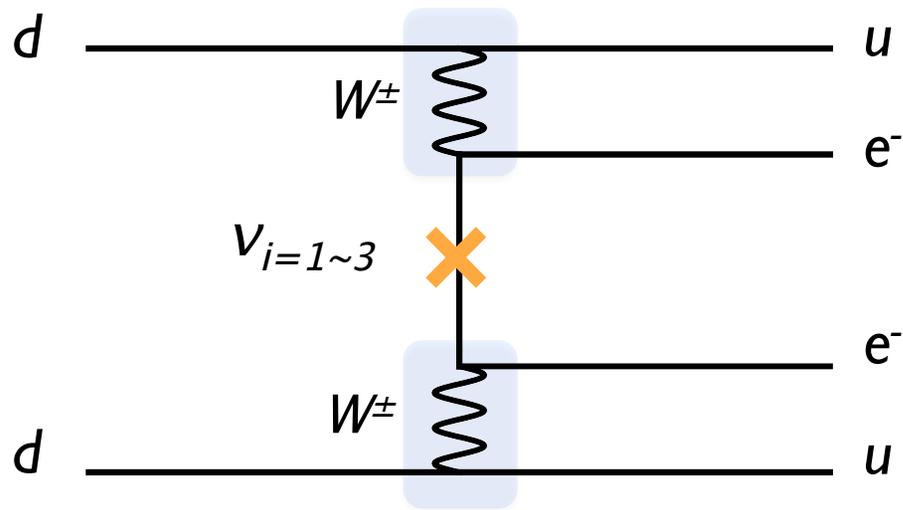
X : Mass insertion

Left-handed vector operator :

$$\mathcal{L}^{(6)} = \frac{G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{VLL}^{(6)} \nu \quad \Bigg| \quad C_{VLL}^{(6)} = -2V_{ud}U_{ei}$$

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$



$$\mathcal{A}_{0\nu 2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left(\sum_{i=1}^3 U_{ei}^2 m_i \right)$$

$O(100) \text{ MeV}$

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$

$$U_{\text{PMNS}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \cdots & \cdots & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

$$\Delta m_{21}^2 = m_2^2 - m_1^2 = 7.39 \times 10^{-5} \text{ [eV}^2\text{]}$$

$$\Delta m_{31}^2 = m_3^2 - m_1^2 = \pm 2.5 \times 10^{-3} \text{ [eV}^2\text{]}$$

From PDG

$$\mathcal{A}_{0\nu 2\beta} \sim \sum_{i=1}^3 U_{ei}^2 \frac{m_i}{q^2 + m_i^2} \sim \frac{1}{q^2} \left(\sum_{i=1}^3 U_{ei}^2 m_i \right)$$

O(100) MeV

Oscillation data

Standard case

Three light Majorana neutrinos : $\nu_{i=1\sim 3}$

$$U_{\text{PMNS}} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ \cdots & \cdots & \cdots \\ \cdots & \cdots & \cdots \end{pmatrix}$$

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$$\Delta m_{31}^2 = m_3^2 - m_1^2 = \pm 2.5 \times 10^{-3} \text{ [eV}^2\text{]}$$

From PDG

Inverse half-life : $\left(T_{1/2}^{0\nu}\right)^{-1} = g_A^4 G_{0\nu} |\mathcal{A}_{0\nu 2\beta}|^2$

$g_A = 1.27$, $G_{0\nu}$: Phase space factor

Search for $0\nu 2\beta$

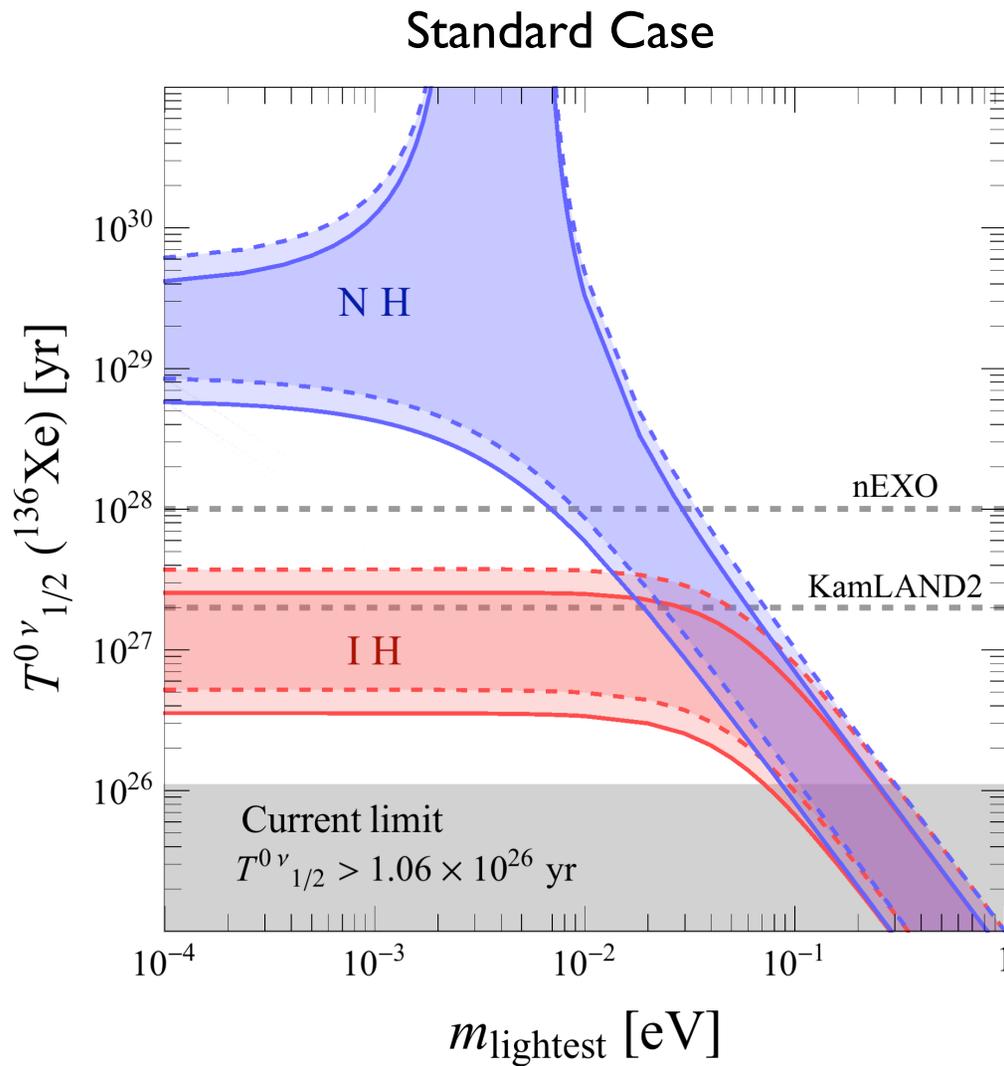
Isotope	Experiment	Current limit ($\times 10^{25}$ yr)		Future sensitivity ($\times 10^{25}$ yr)	
^{48}Ca	ELEGANT-IV	5.8×10^{-3}	[2]	–	
	CANDLES	6.2×10^{-3}	[23]	10^{-2}	[28]
	NEMO-3	2.0×10^{-3}	[9]		
^{76}Ge	MAJORANA DEMONSTRATOR	2.7	[22]	–	
	GERDA	9.0	[24]	–	
	LEGEND	–		10^3	[29]
^{82}Se	CUPID	3.5×10^{-1}	[25]		
	NEMO-3	2.5×10^{-2}	[20]		
	SuperNEMO	–		10	[30]
^{96}Zr	NEMO-3	9.2×10^{-4}	[3]		
^{100}Mo	NEMO-3	1.1×10^{-1}	[8]		
	CUPID-1T	–		9.2×10^2	[37]
	AMoRE	9.5×10^{-3}	[26]	5.0×10	[31]
^{116}Cd	NEMO-3	1.0×10^{-2}	[13]		
^{128}Te	–	1.1×10^{-2}	[1]	–	
^{130}Te	CUORE	3.2	[21]	9.0	[32]
	SNO+	–		1.0×10^2	[33]
^{136}Xe	KamLAND-Zen	10.7	[10]	2.0×10^2	
	EXO-200	3.5	[27]	10^3	[34]
	NEXT	–		2.0×10^2	[35]
	PandaX	–		1.0×10^2	[36]
^{150}Nd	NEMO-3	2.0×10^{-3}	[12]		



$$T_{1/2}^{0\nu} (^{136}\text{Xe}) > 1.06 \times 10^{26} \text{ yr}$$

KamLAND-Zen
PRL117(2016) 082503

Current limit on half-life



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

Inverted Hierarchy (IH)

$$m_3 < m_1 < m_2$$

* Bands

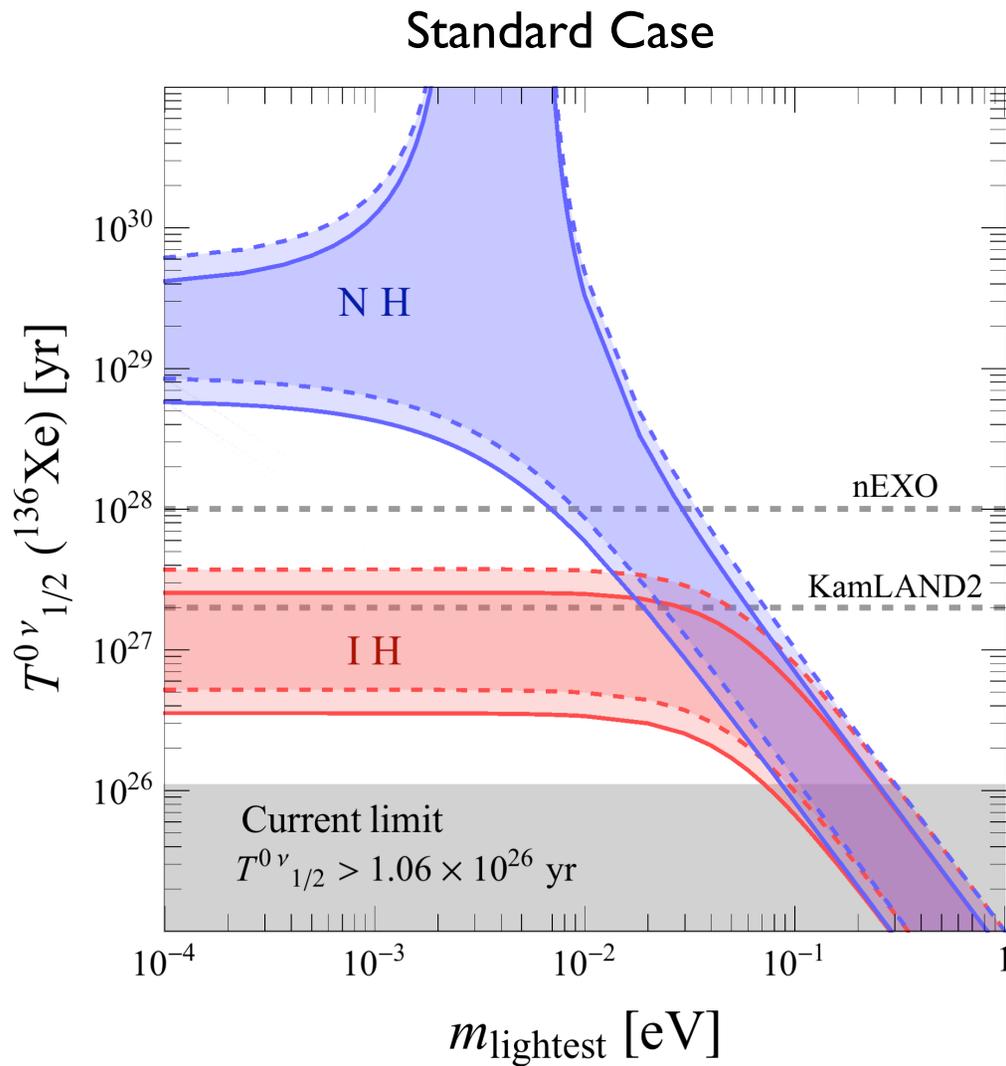
1) Majorana phase

2) Matrix elements

— QRPA

- - - Shell

Current limit on half-life



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

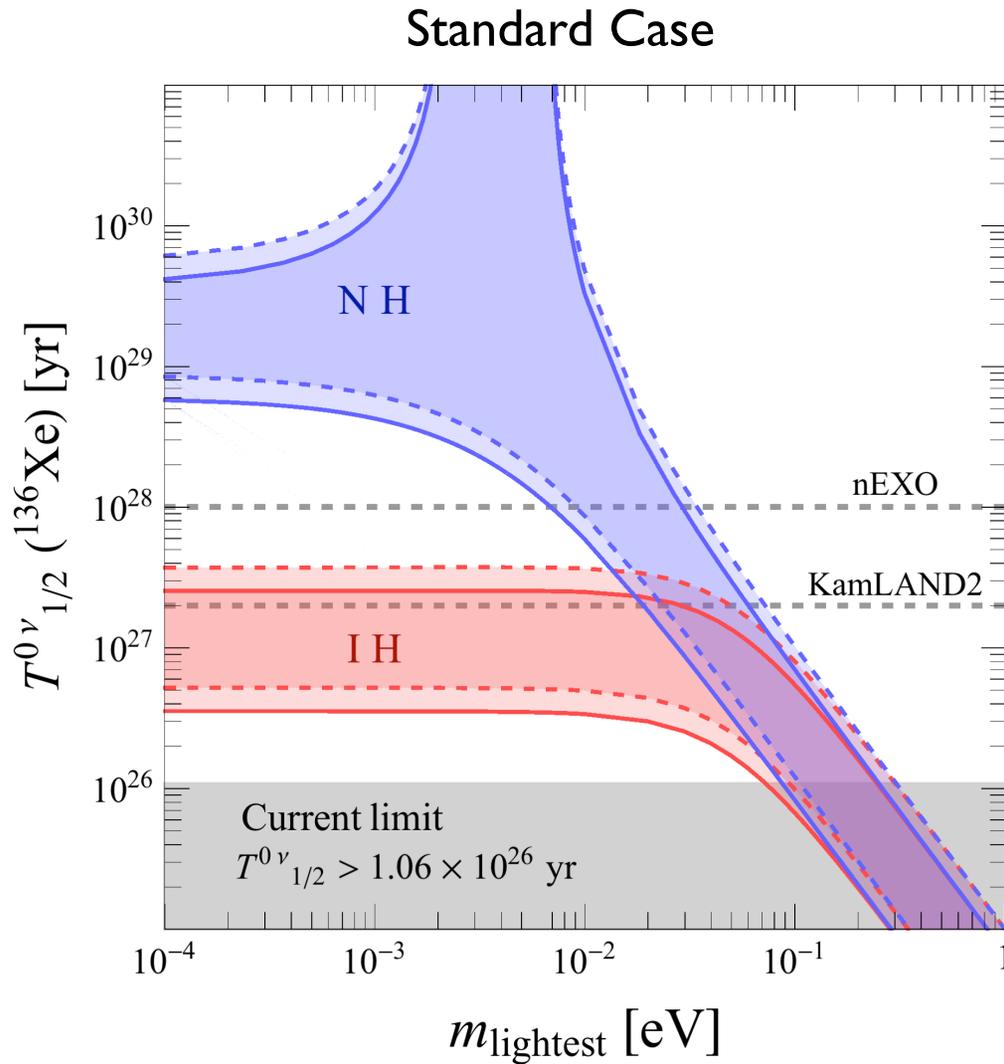
Inverted Hierarchy (IH)

$$m_3 < m_1 < m_2$$

Ruled out :

$$0.1 \text{ eV} \lesssim m_{\text{lightest}}$$

Current limit on half-life



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

Inverted Hierarchy (IH)

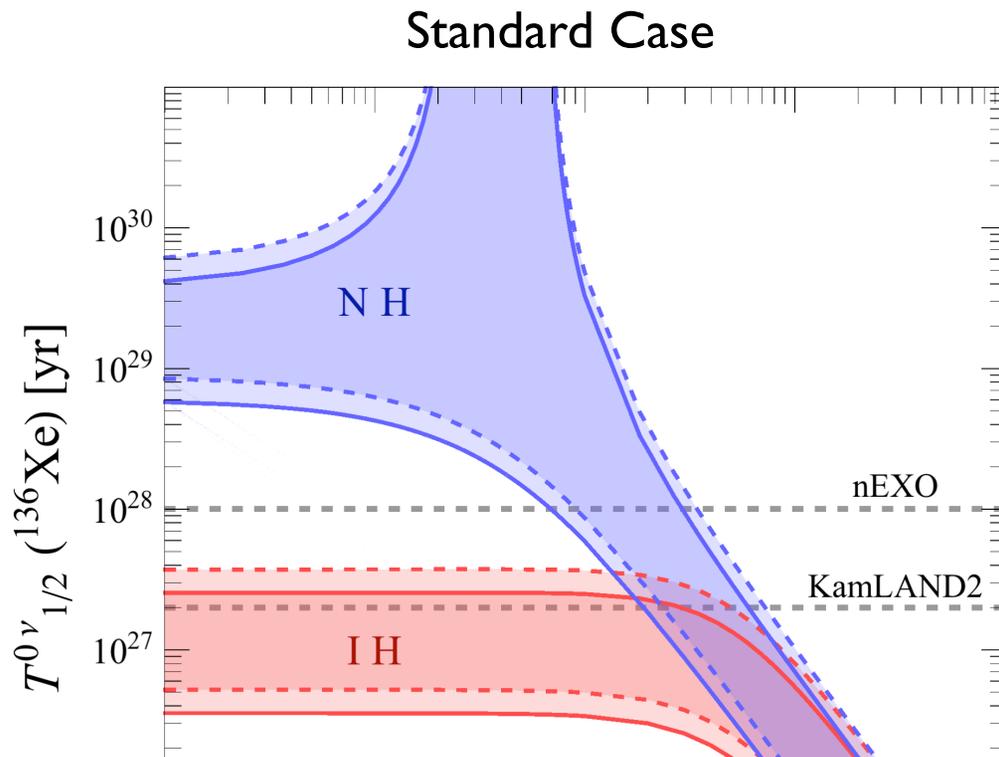
$$m_3 < m_1 < m_2$$

★ Future sensitivity

$$\sim 10^{27} \text{ yr} \quad : \text{KamLAND2-Zen}$$

$$\sim 10^{28} \text{ yr} \quad : \text{nEXO}$$

Current limit on half-life



Normal Hierarchy (NH)

$$m_1 < m_2 < m_3$$

Inverted Hierarchy (IH)

$$m_3 < m_1 < m_2$$

★ Future sensitivity

Standard case : Three light Majorana neutrinos ($M_R \gg v$)

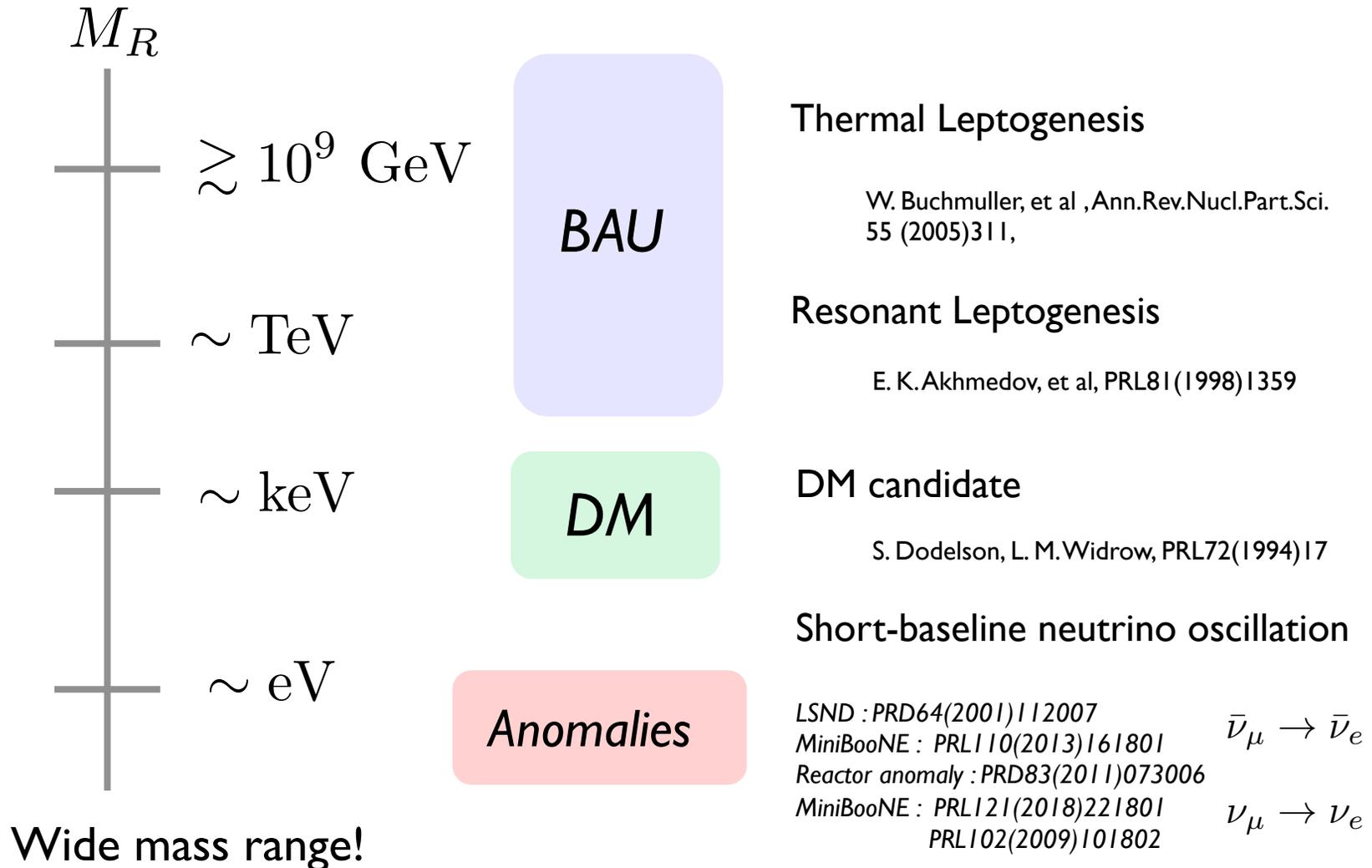
2-Zen

What about light M_R case?

Beyond the standard case

For more details, see
M. Drewes, 1303.6912

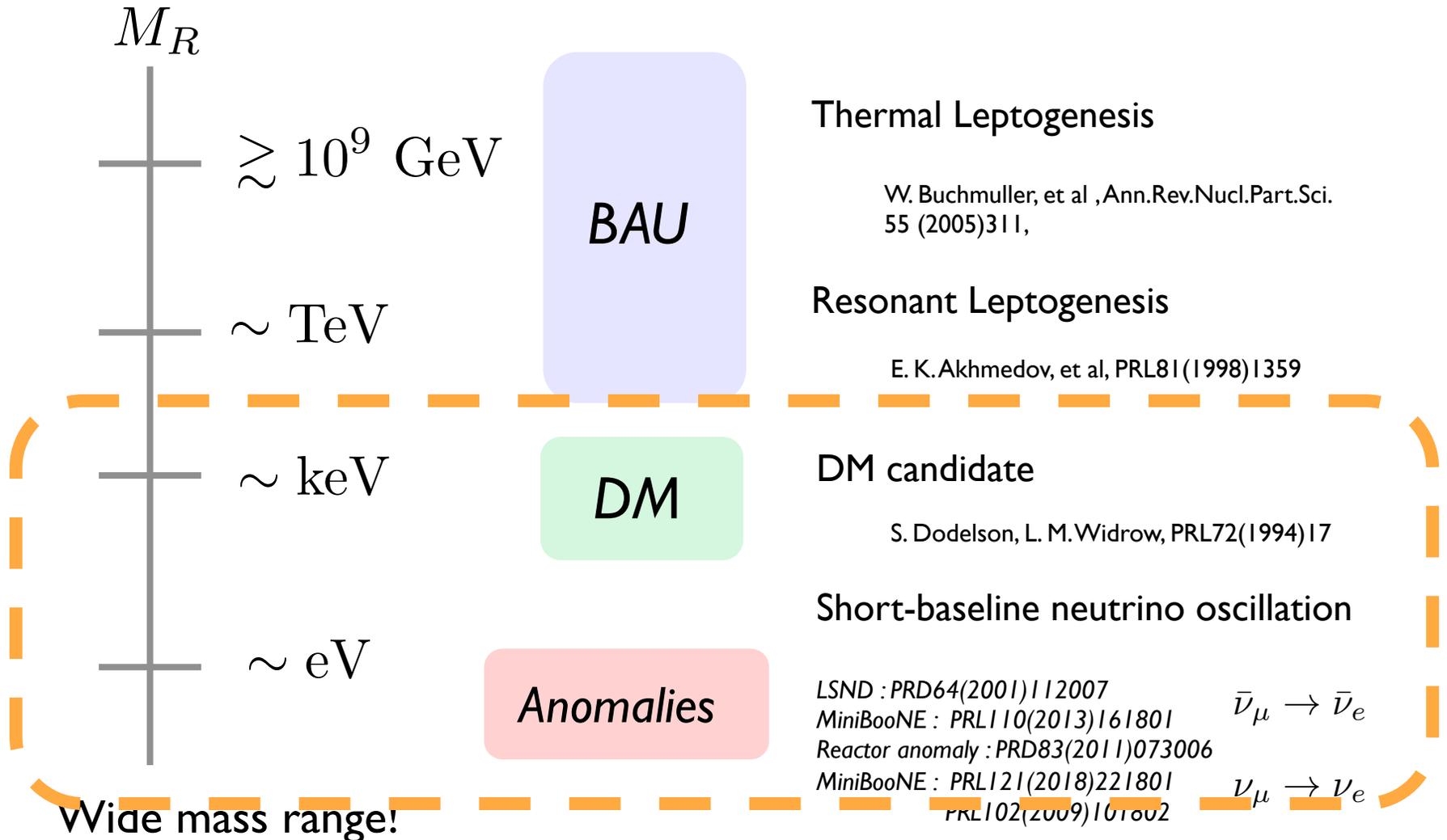
Other phenomenological aspects:



Beyond the standard case

For more details, see
M. Drewes, 1303.6912

* Need theoretical analysis in light of light sterile neutrinos



Our study



Model-independent analysis in the light V_R scenario

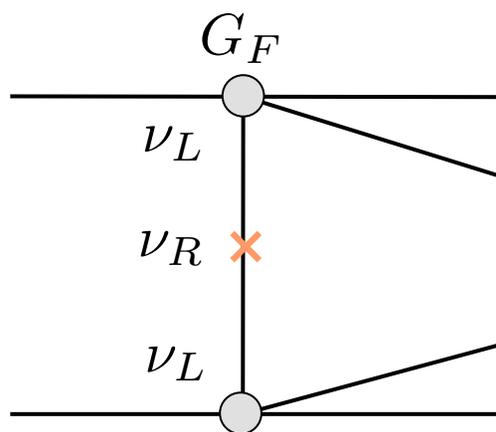
~ Effective Field Theory

Our study

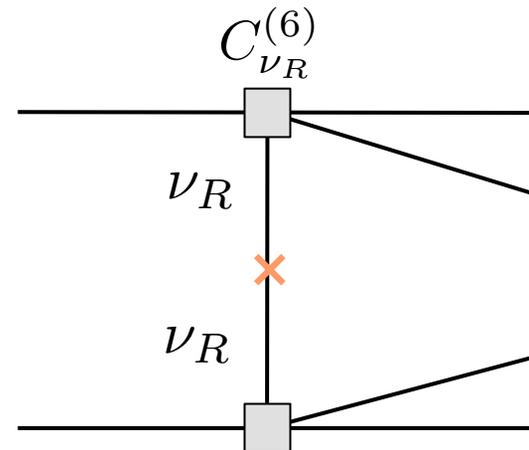
- ★ Model-independent analysis in the light ν_R scenario
 ~ Effective Field Theory

* Non-standard interactions (d = 6)

$$\mathcal{L} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)}$$



VS



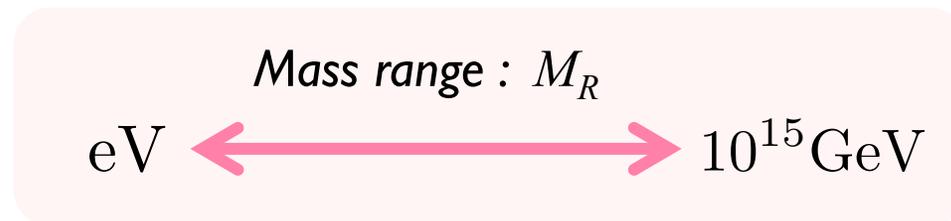
Our study

- ★ Model-independent analysis in the light ν_R scenario
 ~ Effective Field Theory

* Non-standard interactions (d = 6)

$$\mathcal{L} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)}$$

* Derive the master formula depending on M_R

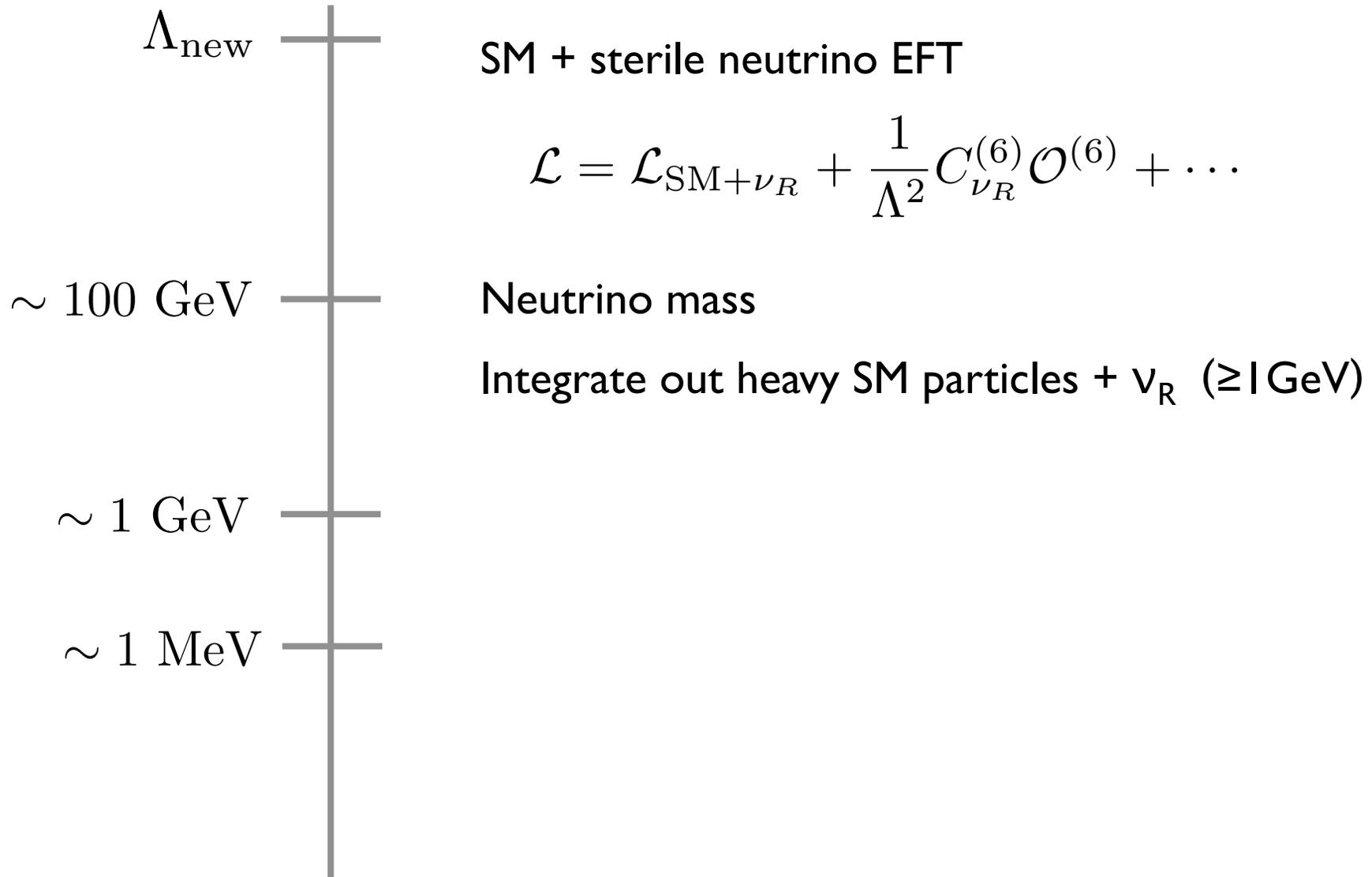


Capture the behavior of light- and high-mass neutrino

SM + Light sterile neutrinos EFT

EFT approach

G. Prezeau, M. Ramsey-Musolf, and P.Vogel, PRD68, 034016 (2003)
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 082(2017)
V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 097(2018)



SM + sterile neutrino EFT

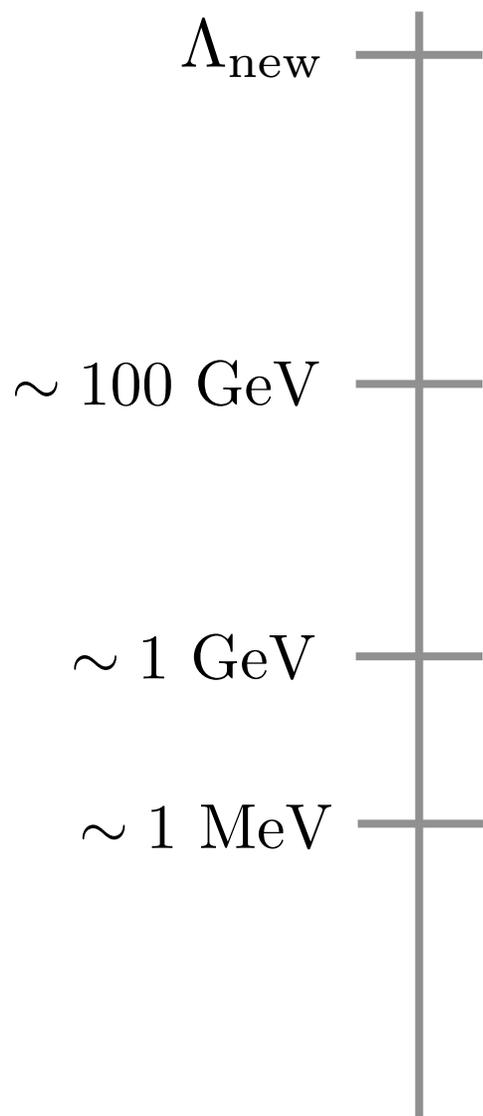
$$\mathcal{L} = \mathcal{L}_{\text{SM}+\nu_R} + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)} + \dots$$

Neutrino mass

Integrate out heavy SM particles + $\nu_R (\geq 1 \text{ GeV})$

EFT approach

G. Prezeau, M. Ramsey-Musolf, and P.Vogel, PRD68, 034016 (2003)
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SM + sterile neutrino EFT

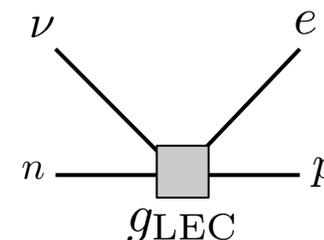
$$\mathcal{L} = \mathcal{L}_{\text{SM}+\nu_R} + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)} + \dots$$

Neutrino mass

Integrate out heavy SM particles + $\nu_R (\geq 1 \text{ GeV})$

$\sim 1 \text{ GeV}$

Chiral Perturbation Theory



$\sim 1 \text{ MeV}$

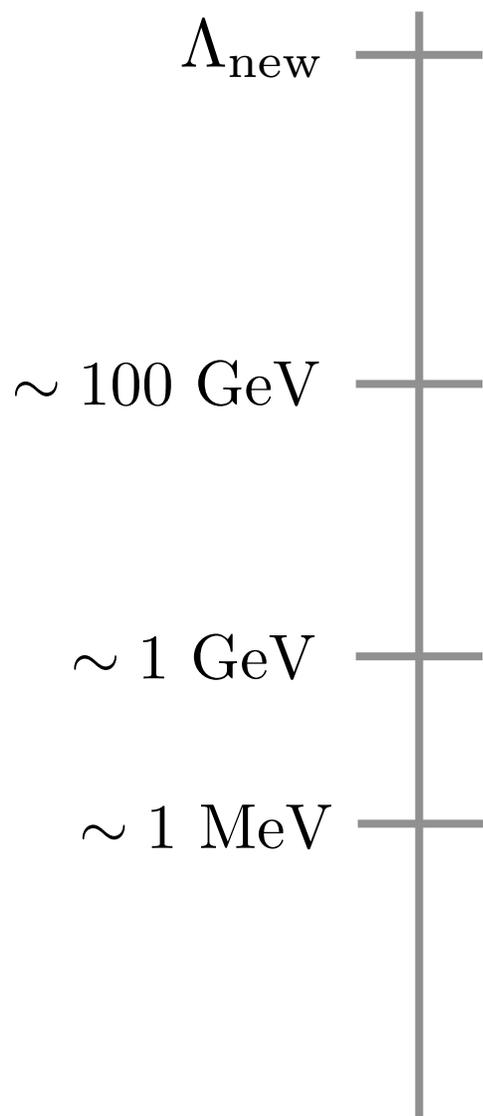
“ Inverse half-life ”

$$\left(T_{1/2}^{0\nu} \right)^{-1} = g_A^4 G_{0\nu} \left| \mathcal{A}_{0\nu 2\beta} \left(g_{\text{LEC}}, C_{\nu_R}^{(6)}, M_{\text{NME}} \right) \right|^2$$

$g_A = 1.27$, $G_{0\nu}$: Phase space factor

EFT approach

G. Prezeau, M. Ramsey-Musolf, and P. Vogel, PRD68, 034016 (2003)
 V. Cirigliano, W. Dekens, J. de Vries, M. L. Graesser, and E. Mereghetti, JHEP 12, 082(2017)
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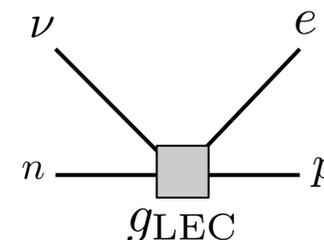
$$\mathcal{L} = \mathcal{L}_{\text{SM}+\nu_R} + \frac{1}{\Lambda^2} C_{\nu_R}^{(6)} \mathcal{O}^{(6)} + \dots$$

Neutrino mass

Integrate out heavy SM particles + ν_R ($\geq 1 \text{ GeV}$)

$\sim 1 \text{ GeV}$

Chiral Perturbation Theory



$\sim 1 \text{ MeV}$

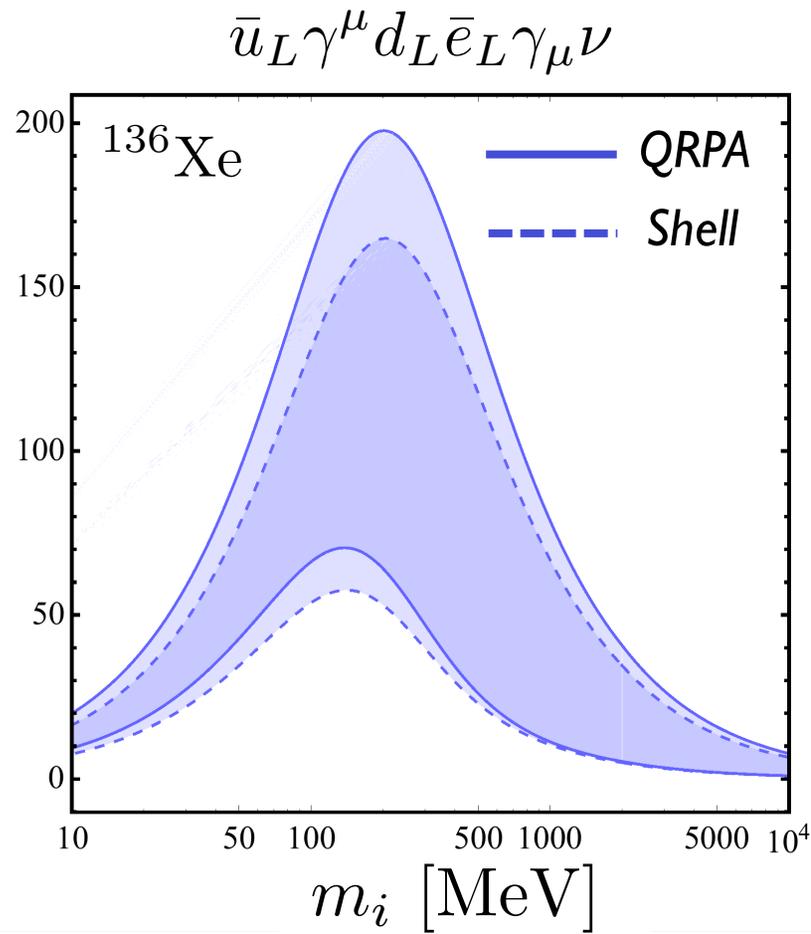
“Inverse half-life”

$$\left(T_{1/2}^{0\nu}\right)^{-1} = g_A^4 G_{0\nu} \left| \mathcal{A}_{0\nu 2\beta} \left(g_{\text{LEC}}, C_{\nu_R}^{(6)}, M_{\text{NME}} \right) \right|^2$$

“Interpolation formulae”

EFT approach

Mass dependence of the amplitude : $|\mathcal{A}_{0\nu 2\beta}(m_i)|_{^{136}\text{Xe}}$



- Two different NMEs
- Peak around $O(100)$ MeV

$$\frac{m_i}{q^2 + m_i^2}$$

$O(100)$ MeV

- Similar behavior in literature

J.Barea, et al PRD92(2015)093001

- Large uncertainty in LECs

1. **Standard interaction**
2. Non-standard interaction
(Leptoquark)

3+1 scenario

One sterile neutrino : m_4

$$\mathcal{L}_{\nu R} = -Y_\nu \bar{L} \tilde{H} \nu_R - \frac{1}{2} \overline{\nu_R^c} M_R \nu_R + \text{H.C}$$

* Standard interactions

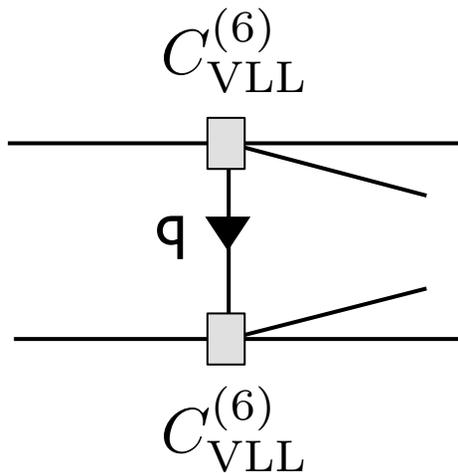
Mass matrix : $(M_\nu)_{i4,4i} \neq 0$

$$M_\nu = \begin{pmatrix} 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ 0 & 0 & 0 & M_D^* \\ M_D^* & M_D^* & M_D^* & M_R \end{pmatrix} \begin{matrix} \text{Yukawa} \\ \text{Majorana} \end{matrix}$$

3+1 scenario

One sterile neutrino : m_4

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{VLL}^{(6)} \nu \quad C_{VLL}^{(6)} = -2V_{ud}U_{ij}$$



For $q^2 \gg m_i^2$

$$\sim \frac{m_i}{q^2} U_{ei}^2 \left(1 + \frac{m_i^2}{q^2} + \dots \right)$$

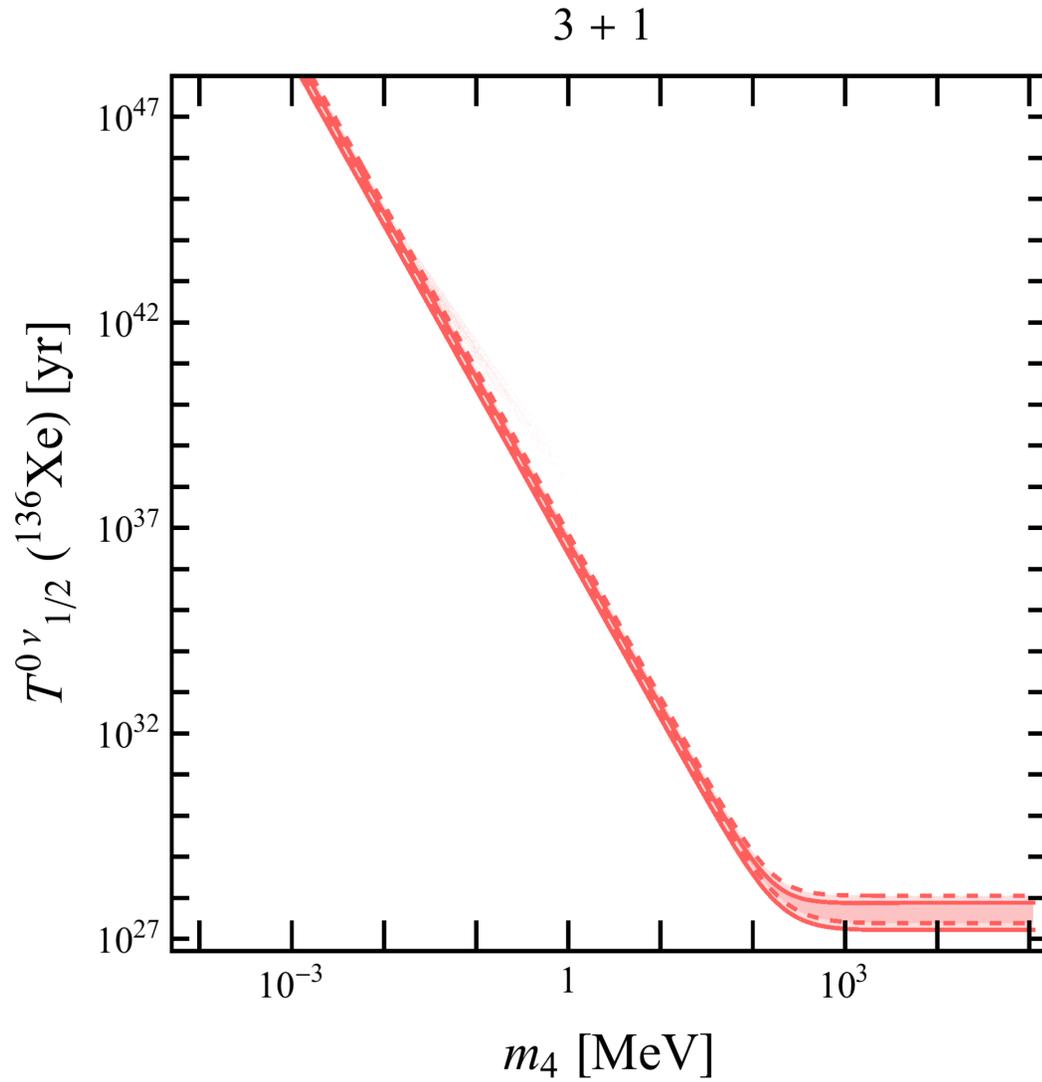
↑ LO vanishes

$$q \sim O(100)\text{MeV}$$

$$m_i U_{ei}^2 = (M_\nu)_{11} = 0$$

* Cancellation of LO contribution in light-mass region

m_4 vs Half-life (^{136}Xe)



The half-life is well above experimental reach.

1. Standard interaction
- 2. Non-standard interaction
(Leptoquark)**

Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)
J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)
I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

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Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **sterile neutrinos**

Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)
J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)
I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

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Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **sterile neutrinos**

Scalar LQ : $\tilde{R} (\mathbf{3}, \mathbf{2}, 1/6)$

$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$

Leptoquark

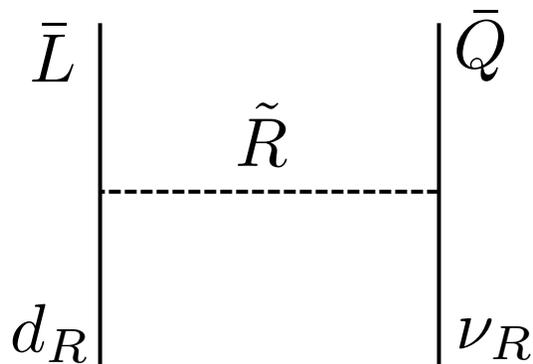
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Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **sterile neutrinos**

Scalar LQ : $\tilde{R} (\mathbf{3}, \mathbf{2}, 1/6)$

$$\mathcal{L}_{LQ} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$



Gauge-invariant dim6 operator:

$$\mathcal{L}_{\nu_R}^{(6)} = C_{LdQ\nu}^{(6)} (\bar{L} d_R) \epsilon (\bar{Q} \nu_R)$$

$$C_{LdQ\nu}^{(6)} = \frac{1}{m_{LQ}^2} y^{\overline{LR}} y^{RL*}$$

Leptoquark

J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 88, 035009 (2013)
J. M. Arnold, B. Fornal and M. B. Wise, Phys. Rev. D 87, 075004 (2013)
I. Dorsner, S. Fajfer, A. Greljo, J. F. Kamenik and N. Kosnik, Phys. Rept. 641, 1 (2016)

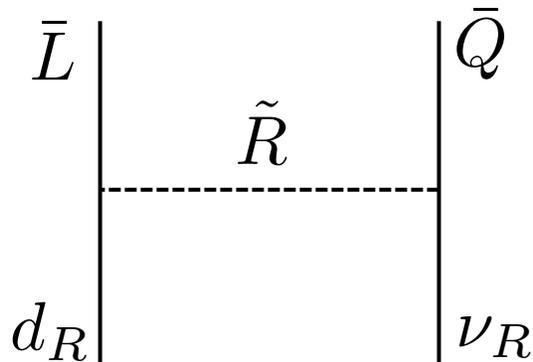
26

Leptoquark (LQ) couples to the SM **quark** and **lepton**

+ **sterile neutrinos**

Scalar LQ : $\tilde{R} (\mathbf{3}, \mathbf{2}, 1/6)$

$$\mathcal{L}_{\text{LQ}} = -y^{RL} \bar{d}_R \tilde{R} \epsilon L + y^{\overline{LR}} \bar{Q} \tilde{R} \nu_R$$



LQ parameters :

$$m_{\text{LQ}} = 10 \text{ TeV} \quad y^{\overline{LR}} y^{RL*} = 1.0$$

Leptoquark

Scalar and tensor operators show up below EW scale:

$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[\bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

$$C_{\text{SRR}}^{(6)} = 4C_{\text{TRR}}^{(6)} = \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{Ni}^* \quad \begin{array}{l} N = 4 \\ i = 1 \sim 4 \end{array}$$

Leptoquark

Scalar and tensor operators show up below EW scale:

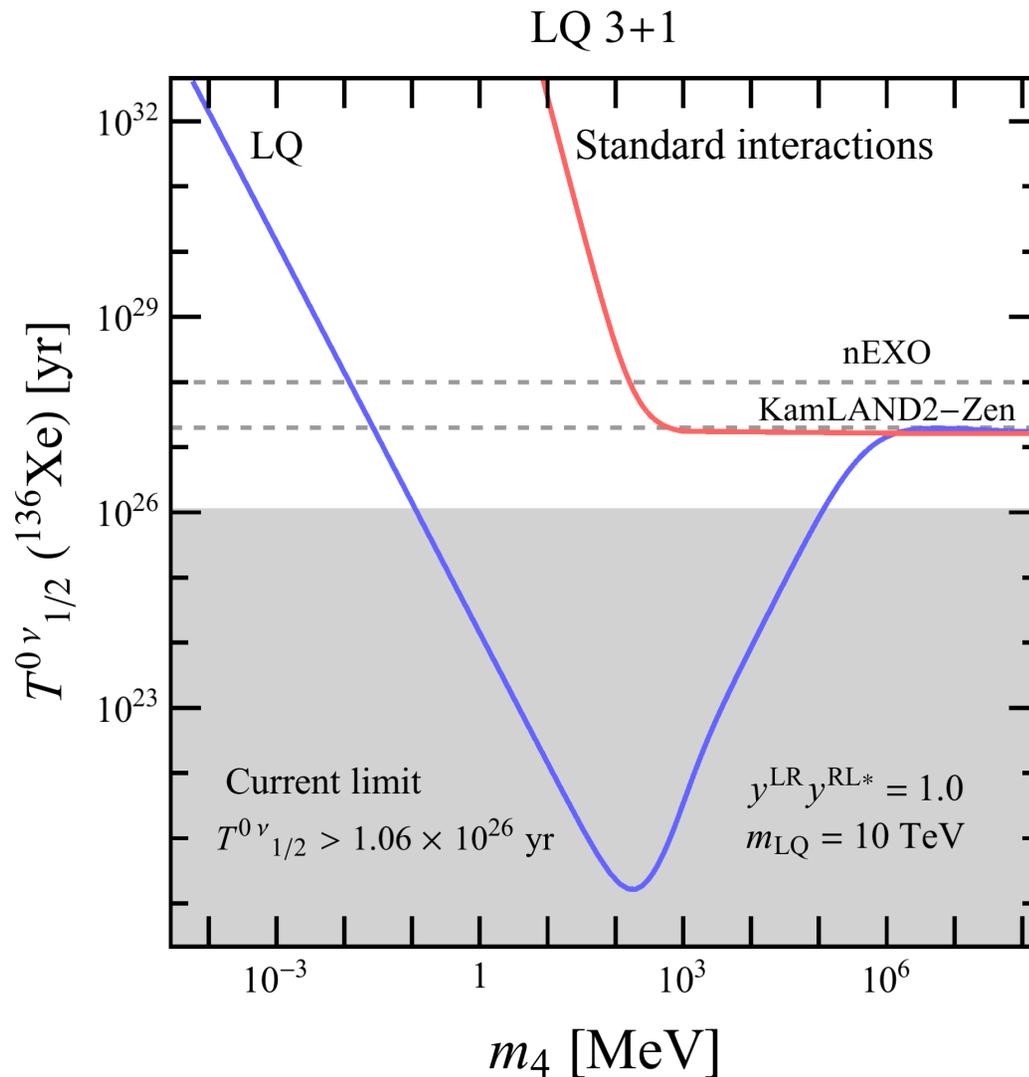
$$\mathcal{L}^{(6)} = \frac{2G_F}{\sqrt{2}} \left[\bar{u}_L d_R \bar{e}_L C_{\text{SRR}}^{(6)} \nu_i + \bar{u}_L \sigma^{\mu\nu} d_R \bar{e}_L \sigma_{\mu\nu} C_{\text{TRR}}^{(6)} \nu_i \right]$$

$$C_{\text{SRR}}^{(6)} = 4C_{\text{TRR}}^{(6)} = \frac{v^2}{2} C_{LdQ\nu}^{(6)} U_{Ni}^* \quad \begin{array}{l} N = 4 \\ i = 1 \sim 4 \end{array}$$

$$+ \frac{2G_F}{\sqrt{2}} \bar{u}_L \gamma^\mu d_L \bar{e}_L \gamma_\mu C_{\text{VLL}}^{(6)} \nu \quad \leftarrow \text{Induced by mixing (No LQ interaction)}$$

$$C_{\text{VLL}}^{(6)} = -2V_{ud} U_{ij} \quad i = 1 \sim 3, j = 1 \sim 4$$

3+1 : m_4 vs Half-life

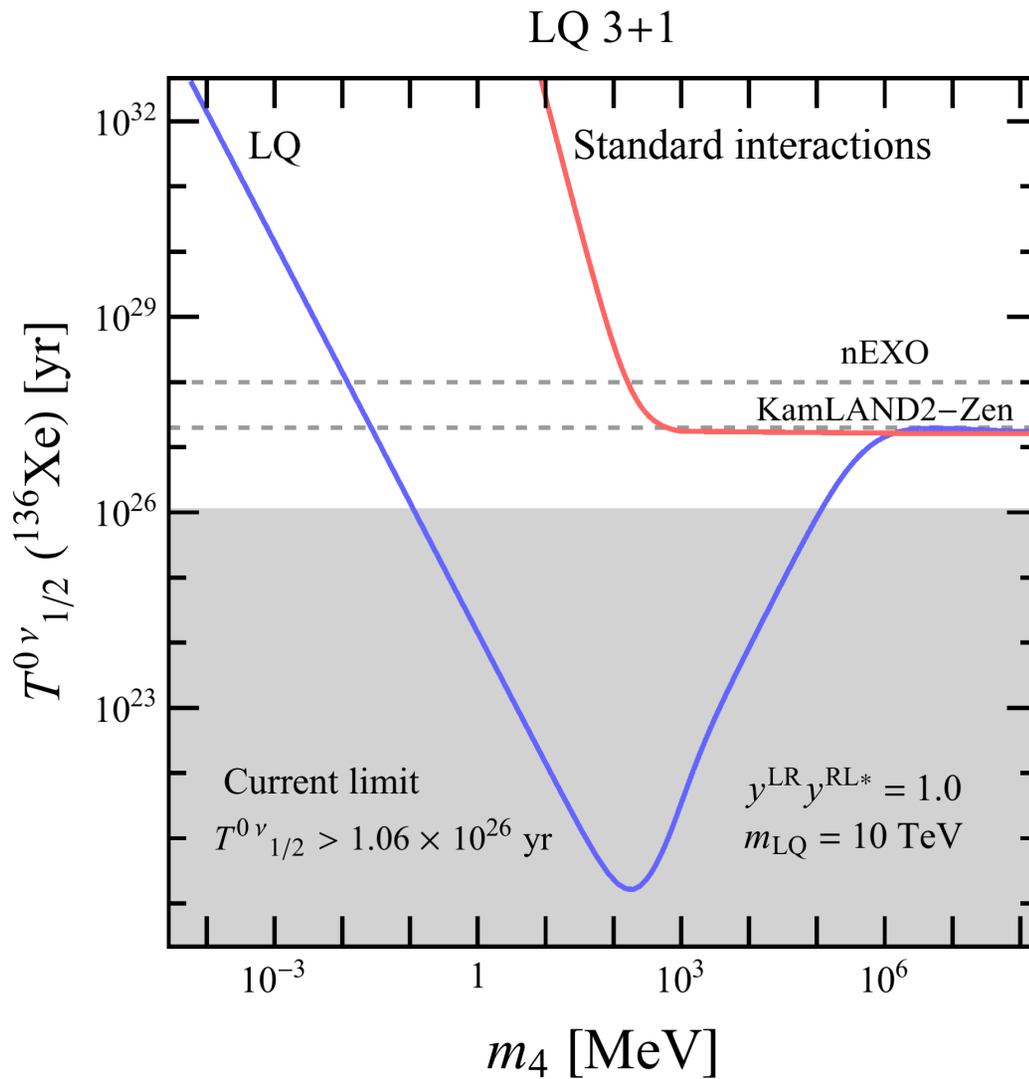


Blue : LQ interaction

Pink : No LQ interaction
 (vector contribution)

* LQ interactions dominate
 over standard contributions.

3+1 : m_4 vs Half-life

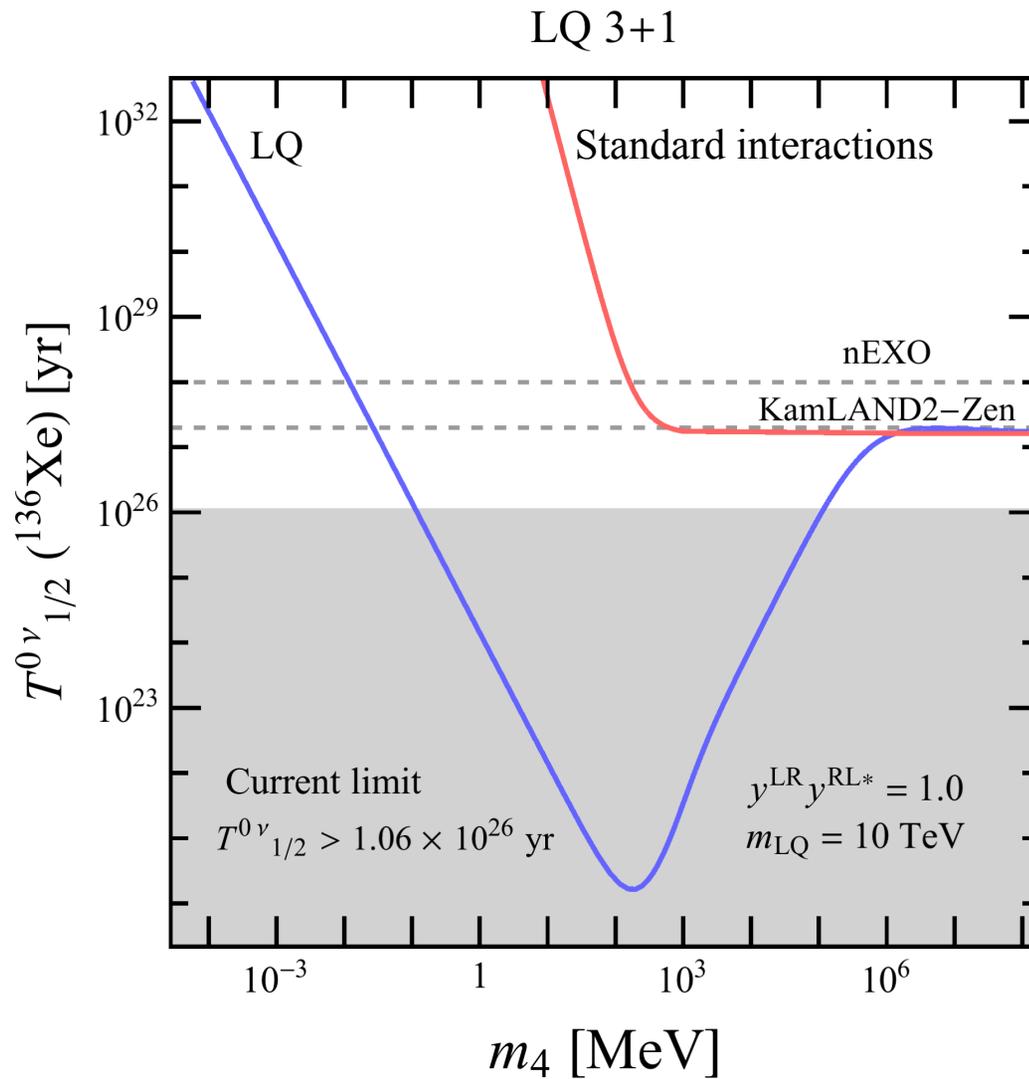


Blue : LQ interaction

Pink : No LQ interaction
(vector contribution)

$0.1 \text{ MeV} \lesssim m_4 \lesssim 100 \text{ GeV}$

3+1 : m_4 vs Half-life



Future sensitivity

$\sim 10^{27}$ yr : KamLAND2-Zen

$\sim 10^{28}$ yr : nEXO

$$m_4 \gtrsim 10 \text{ keV}$$

Tau to e transition

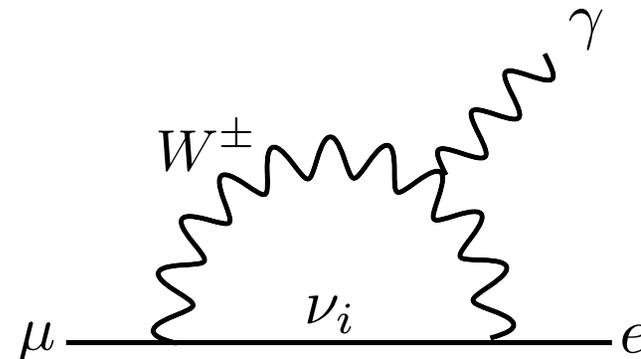
CLFV

Nonzero neutrino mass induces CLFV.

Ex) Minimal extension of the SM

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\nu\text{-mass}}$$

Dirac or Majorana



Petcov '77, Marciano-Sanda '77

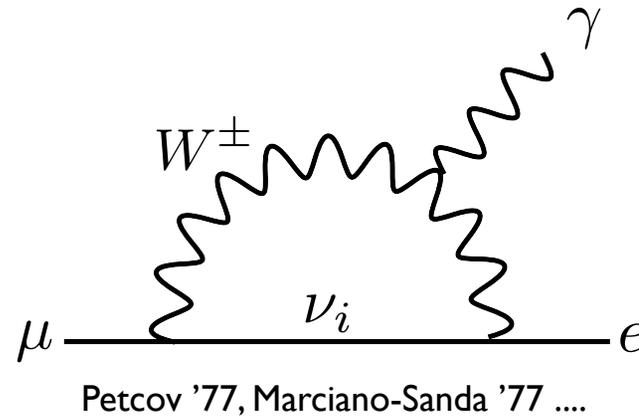
CLFV

Nonzero neutrino mass induces CLFV.

Ex) Minimal extension of the SM

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\nu\text{-mass}}$$

Dirac or Majorana



$$\text{Br}(\mu \rightarrow e\gamma) = \frac{3\alpha_{\text{em}}}{32\pi} \left| \sum_{i=2,3} U_{\mu i}^* U_{ei} \frac{\Delta m_{1i}^2}{m_W^2} \right|^2 < 10^{-54}$$

Extremely small!

The predicted BR is too small to be observed.

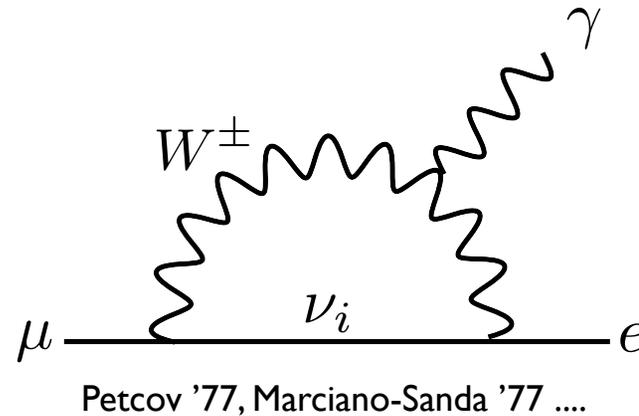
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Extremely small!

The observation of CLFV would imply another contribution.

Present searches

CLFV searches have been ongoing.

* Example



$$\text{BR}(\mu^+ \rightarrow e^+ \gamma) < 4.2 \times 10^{-13}$$

MEG Collaboration, Eur. Phys. J. C 76(8), 434 (2016).

$$\text{BR}(\mu^- \text{ Au} \rightarrow e^- \text{ Au}) < 7 \times 10^{-13}$$

SINDRUM II, Eur. Phys. J. C 47(2), 337–346 (2006).

$$\text{BR}(\mu^+ \rightarrow e^+ e^- e^+) < 1 \times 10^{-12}$$

SINDRUM, Nucl. Phys. B 299 (1988) 1-6

Present searches

CLFV searches have been ongoing.

* Example



$$\text{BR}(\mu^+ \rightarrow e^+ \gamma) < 4.2 \times 10^{-13}$$

$$\text{BR}(\mu^- \text{ Au} \rightarrow e^- \text{ Au}) < 7 \times 10^{-13}$$

$$\text{BR}(\mu^+ \rightarrow e^+ e^- e^+) < 1 \times 10^{-12}$$

Future limit $< 6 \times 10^{-14}$



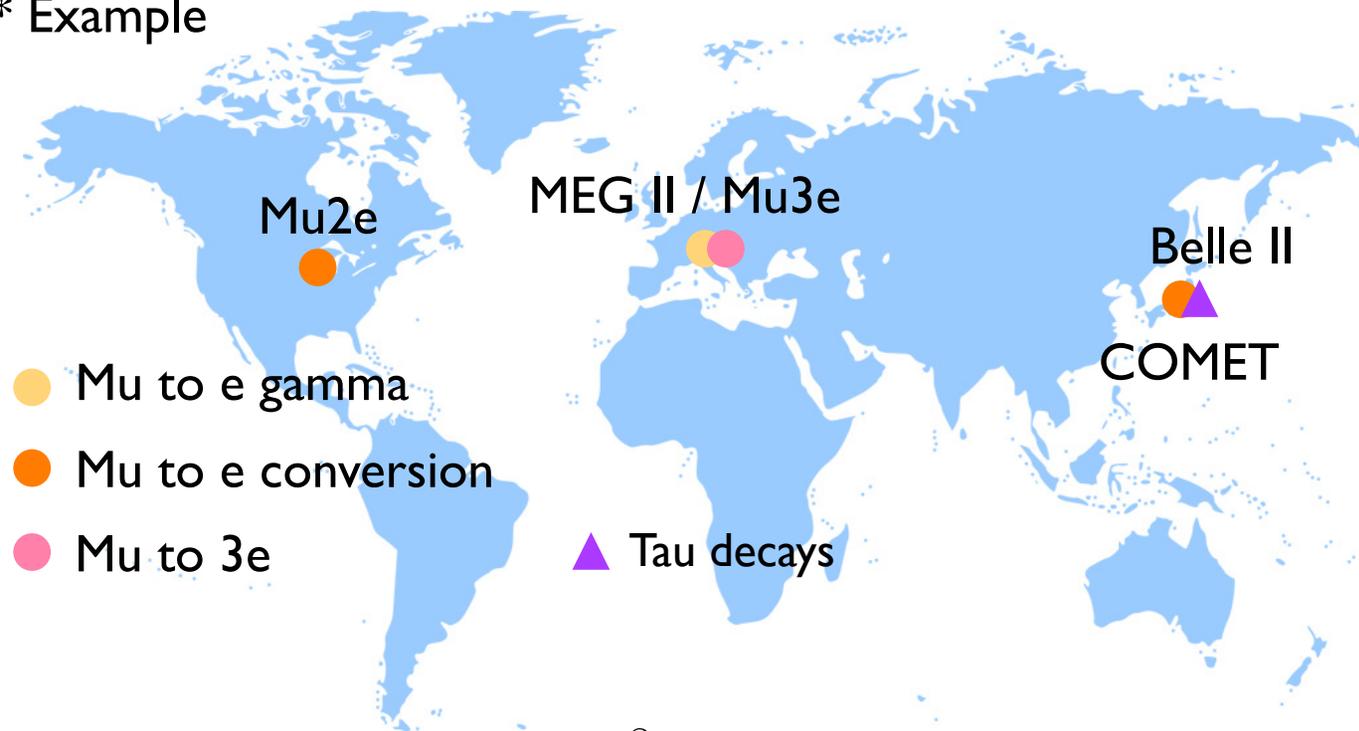
$$< 3 \times 10^{-17}$$

$$< 2 \times 10^{-15}$$

Present searches

CLFV searches have been ongoing.

* Example



$$\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$$

BaBar, Phys.Rev.Lett. 104 (2010) 021802

$$\text{BR}(\tau \rightarrow e\pi^+\pi^-) < 2.3 \times 10^{-8}$$

Belle, Phys.Lett.B 719 (2013) 346-353

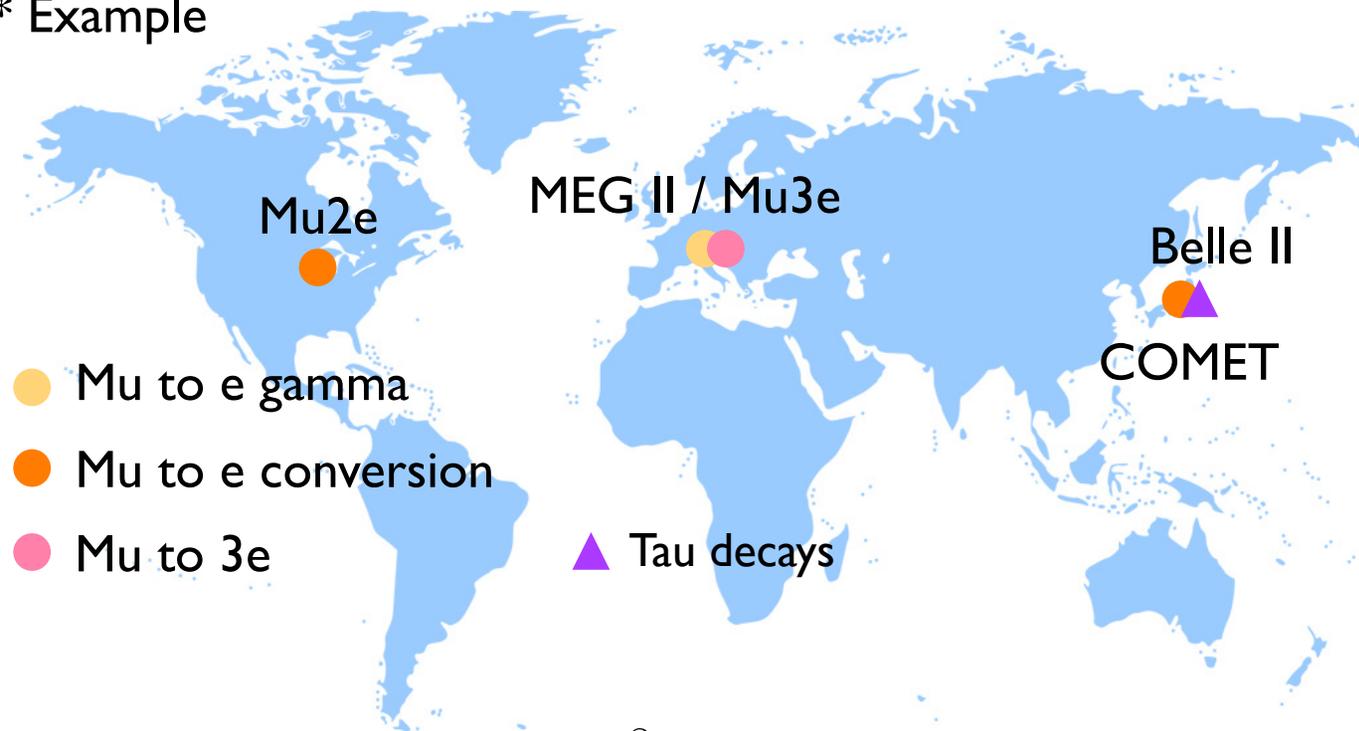
$$\text{BR}(\tau \rightarrow e\pi^0) < 8 \times 10^{-8}$$

Belle, Phys.Lett.B 648 (2007) 341-350

Present searches

CLFV searches have been ongoing.

* Example



$$\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$$

$$\text{BR}(\tau \rightarrow e\pi^+\pi^-) < 2.3 \times 10^{-8}$$

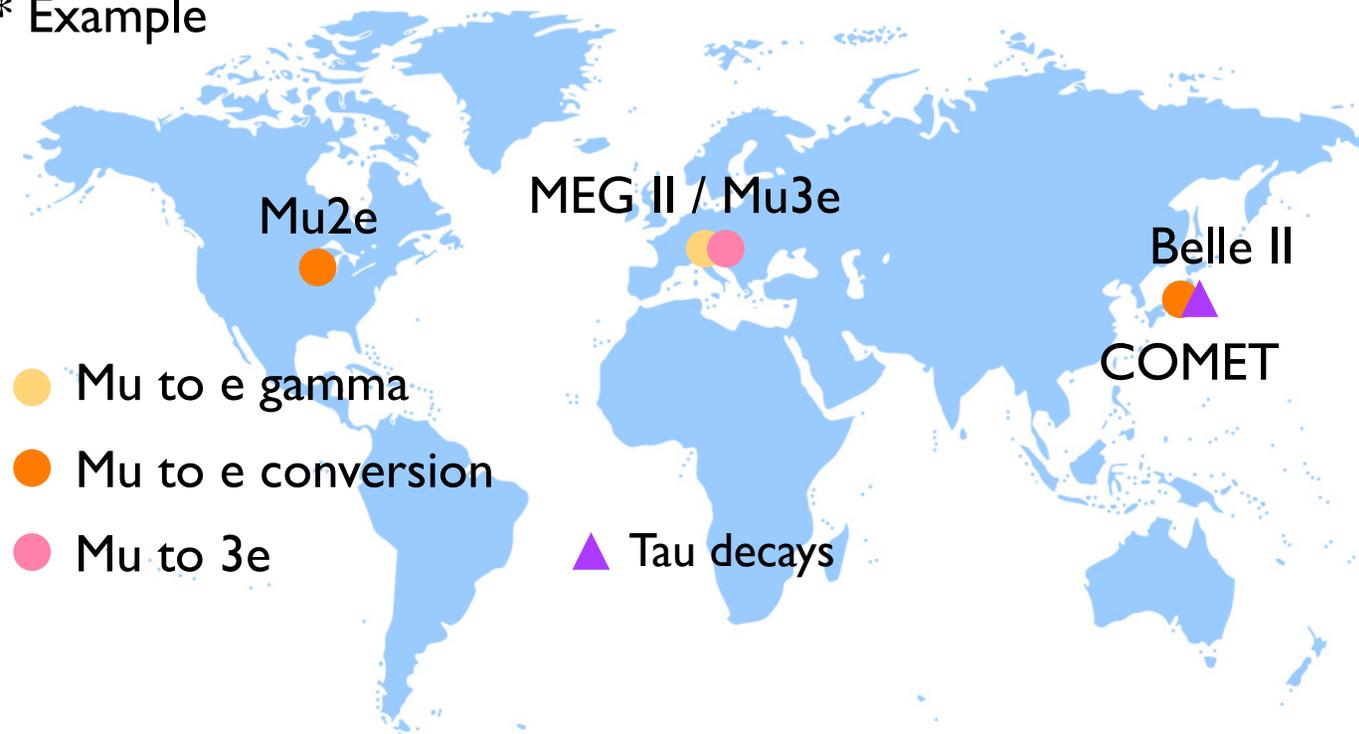
$$\text{BR}(\tau \rightarrow e\pi^0) < 8 \times 10^{-8}$$

Semileptonic tau decays

Present searches

CLFV searches have been ongoing.

* Example

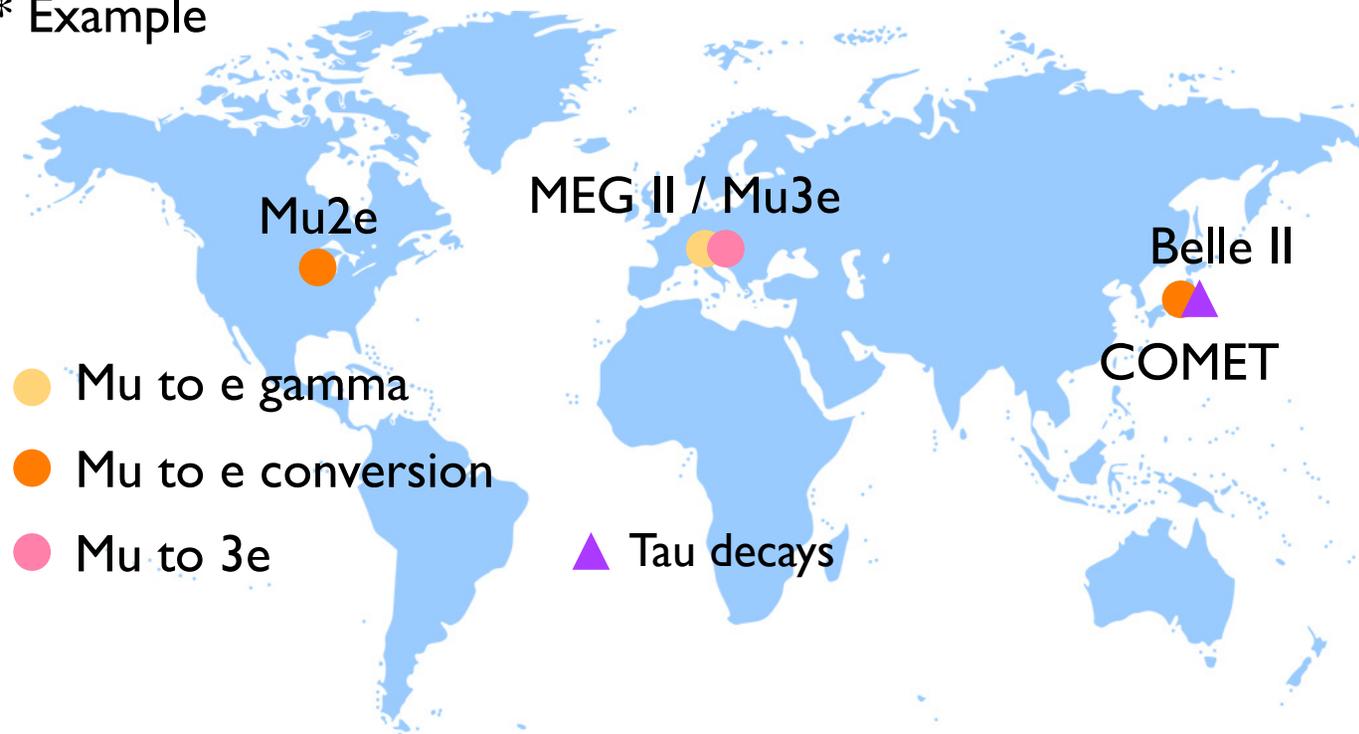


Tau-e LFV : Weaker constraints
 Rich variety of LFV tau decays

Present searches

CLFV searches have been ongoing.

* Example



Tau-e LFV : BR $\sim O(10^{-(9-10)})$ at Belle II

What about high-energy probes?

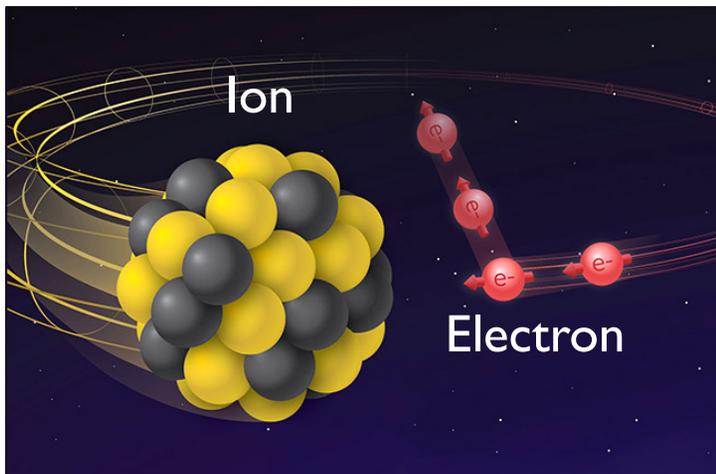
Electron-Ion Collider

EIC Detector Requirements and R&D Handbook
EIC Yellow report, arXiv:2103.05419

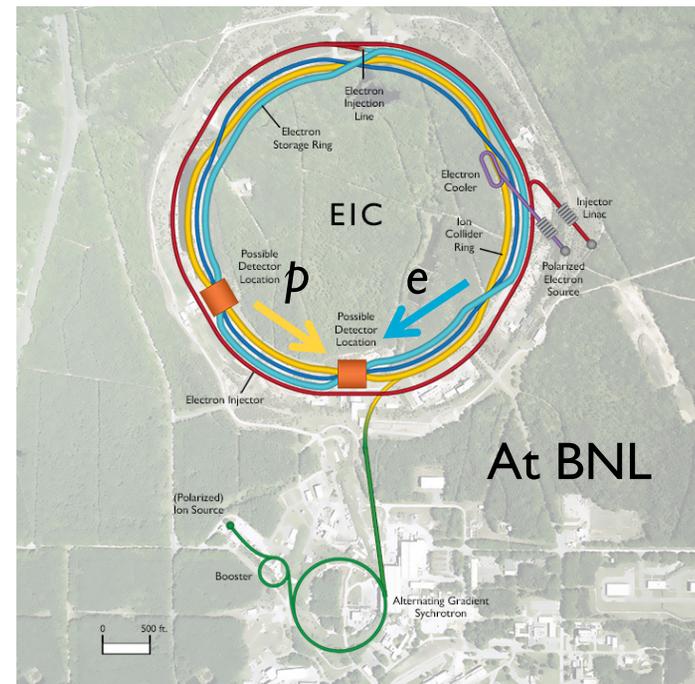
19

★ One potential probe : LFV search at the EIC

DOE granted CD-0 to the EIC on January 9, 2020.



Collide electrons and protons/heavy ions



Map the structure of the proton and nuclei

- Electrons - protons/heavy ions collisions

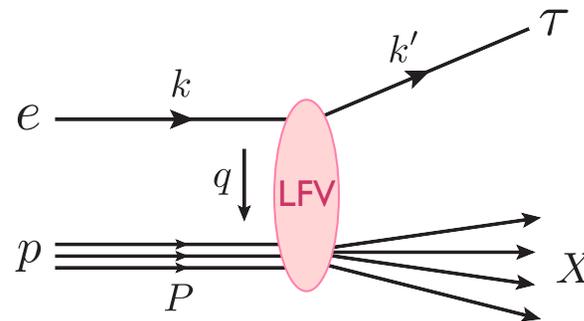
$$\sqrt{S} = 20 \sim 100 \text{ GeV} \quad (\text{Upgradable to } 140 \text{ GeV})$$

- Polarized electron (~70%) and proton (~70%) beams

- High Luminosity

$$\mathcal{L} \sim 10^{33-34} \text{ cm}^{-2} \text{ s}^{-1}$$

(10-100 fb⁻¹ per year)



(e.g. HERA $\sqrt{S} = 318 \text{ GeV}$, $\mathcal{L} = 1.4 \times 10^{31} \text{ cm}^{-1} \text{ s}^{-1}$)

Another opportunity to search for $ep \rightarrow \tau X$

Our study

ArXiv: 2102.06176

V. Cirigliano, KF, C. Lee, E. Mereghetti, B. Yan (LANL)



Study the possibility to probe e-tau LFV at the EIC

* Tau-e interactions in SMEFT ($d = 6$)

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} C_{\tau e}^{(6)} \mathcal{O}^{(6)}$$

Tau-e LFV interaction

Our study

ArXiv: 2102.06176

V. Cirigliano, KF, C. Lee, E. Mereghetti, B. Yan (LANL)

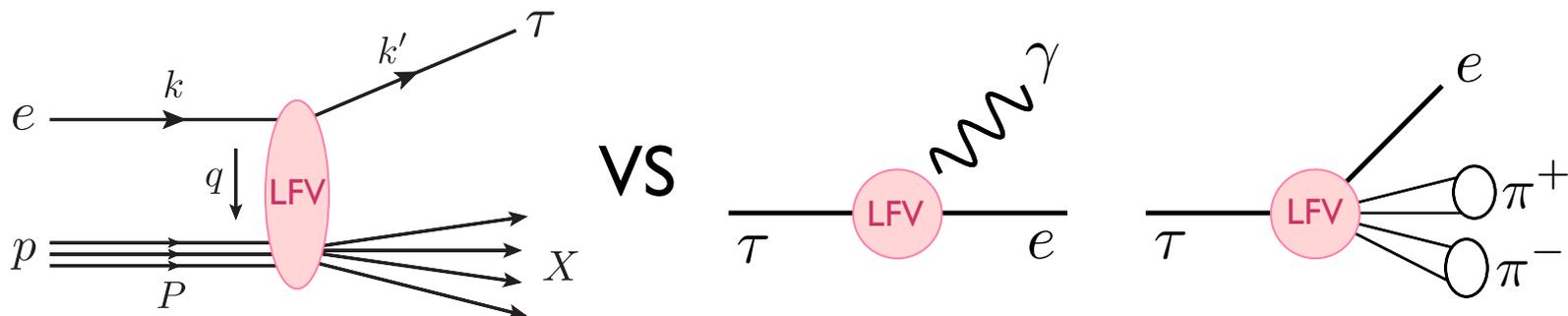
★ Study the possibility to probe e-tau LFV at the EIC

* Tau-e interactions in SMEFT ($d = 6$)

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda^2} C_{\tau e}^{(6)} \mathcal{O}^{(6)}$$

Tau-e LFV interaction

* Current limits on tau-e operators



EFT approach

Total : 16 different LFV operators

$$\mathcal{L}_{\text{LFV}} = \mathcal{L}_{\psi^2 \varphi^2 D} + \mathcal{L}_{\psi^2 X \varphi} + \mathcal{L}_{\psi^2 \varphi^3} + \mathcal{L}_{\psi^4}$$

X : Gauge boson ψ : Fermion φ : Higgs

Results

Total : 16 different LFV operators

Ex) Dipole, Yukawa and 4F vector operators

$$\mathcal{L}_{\text{LFV}} \supset -\frac{e}{2v} (\Gamma_{\gamma}^e)_{\tau e} \bar{\tau}_L \sigma^{\mu\nu} e_R F_{\mu\nu}$$

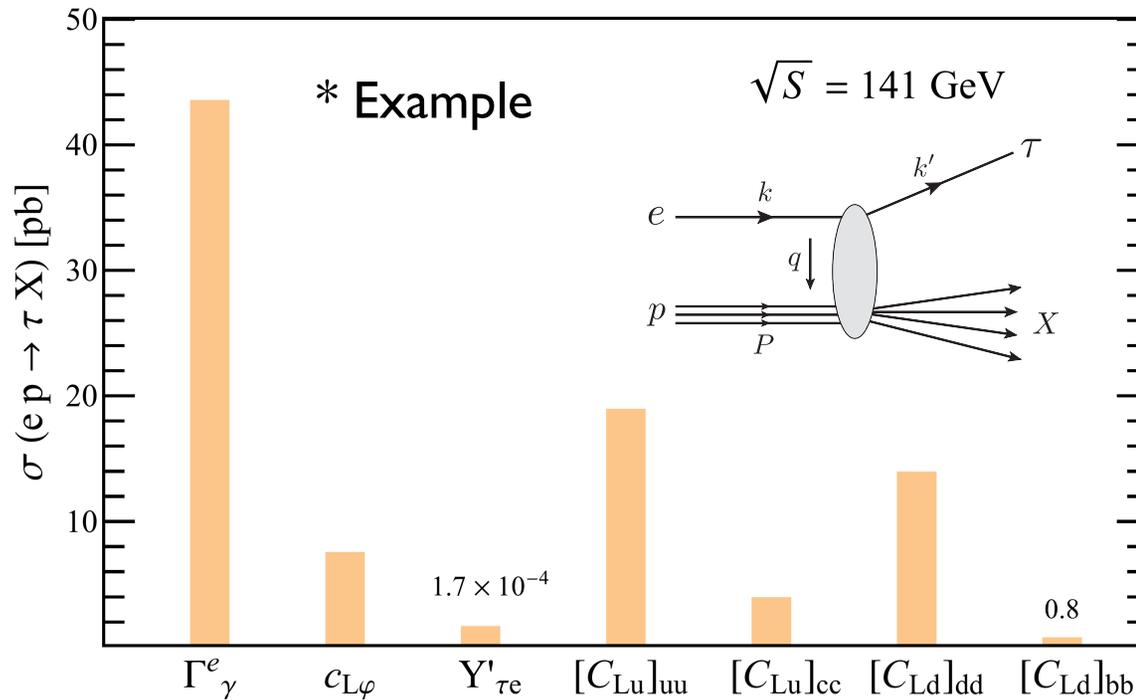
Photon dipole

$$-\frac{4G_F}{\sqrt{2}} [C_{Lu}]_{cc} \bar{\tau}_L \gamma^{\mu} e_L \bar{c}_R \gamma_{\mu} c_R \quad \text{VLR : cc element}$$

$$-\frac{4G_F}{\sqrt{2}} [C_{Ld}]_{bb} \bar{\tau}_L \gamma^{\mu} e_L \bar{b}_R \gamma_{\mu} b_R \quad \text{VLR : bb element}$$

* Single-operator analysis

Unpolarized cross sections at LO in QCD (C=1)

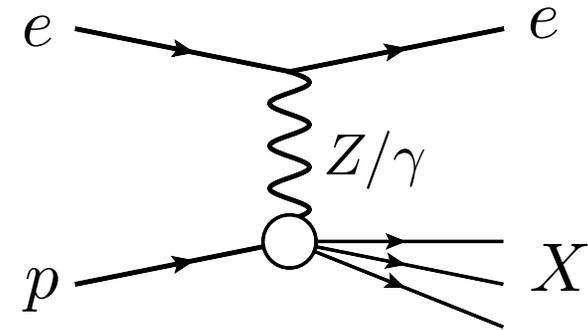


- Mostly pb range
 - Heavy quarks suppressed by PDF
- Larger PDF/scale uncertainties, e.g. 0.8 (0.5) pb for $[C_{Ld}]_{bb}$

EIC analysis

- Major backgrounds

- 1) Neutral Current : $ep \rightarrow ej$
- 2) Charged Current : $ep \rightarrow \nu_e j$

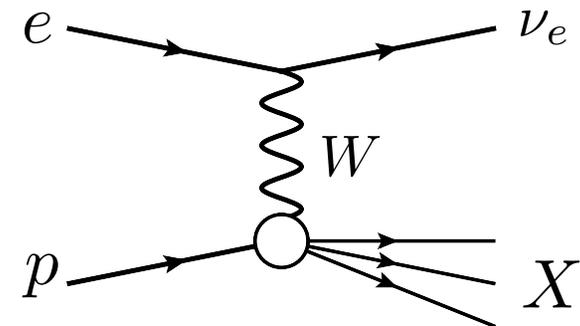


- Tau decays

$$\text{BR}(\tau \rightarrow e\bar{\nu}_e\nu_\tau) = 17.82\%$$

$$\star \text{BR}(\tau \rightarrow \mu\bar{\nu}_\mu\nu_\tau) = 17.39\%$$

$$\text{BR}(\tau \rightarrow X_h\nu_\tau) = 64.8\%$$



✓ Consider simple cuts to enhance efficiencies

LFV tau and meson decays

Limits on quark-flavor conserving operators

Decay mode	Upper limit (90% C.L.)	
$\tau \rightarrow e\gamma$	3.3×10^{-8}	
$\tau \rightarrow e\pi^+\pi^-$	2.3×10^{-8}	
$\tau \rightarrow e\pi^0$	8.0×10^{-8}	
$\tau \rightarrow e\eta$	9.2×10^{-8}	BR $\sim \mathcal{O}(10^{-8})$
$\tau \rightarrow e\eta'$	1.6×10^{-7}	
$\tau \rightarrow ee^+e^-$	2.7×10^{-8}	
$\tau \rightarrow e\mu^+\mu^-$	2.7×10^{-8}	

LFV tau and meson decays

Limits on quark-flavor conserving operators

	Decay mode	Upper limit (90% C.L.)
	$\tau \rightarrow e\gamma$	3.3×10^{-8}
Semileptonic (uu/dd/ss)	$\tau \rightarrow e\pi^+\pi^-$	2.3×10^{-8}
	$\tau \rightarrow e\pi^0$	8.0×10^{-8}
	$\tau \rightarrow e\eta$	9.2×10^{-8}
	$\tau \rightarrow e\eta'$	1.6×10^{-7}
		$\tau \rightarrow ee^+e^-$
Leptonic	$\tau \rightarrow e\mu^+\mu^-$	2.7×10^{-8}

LFV tau and meson decays

Limits on quark-flavor conserving operators

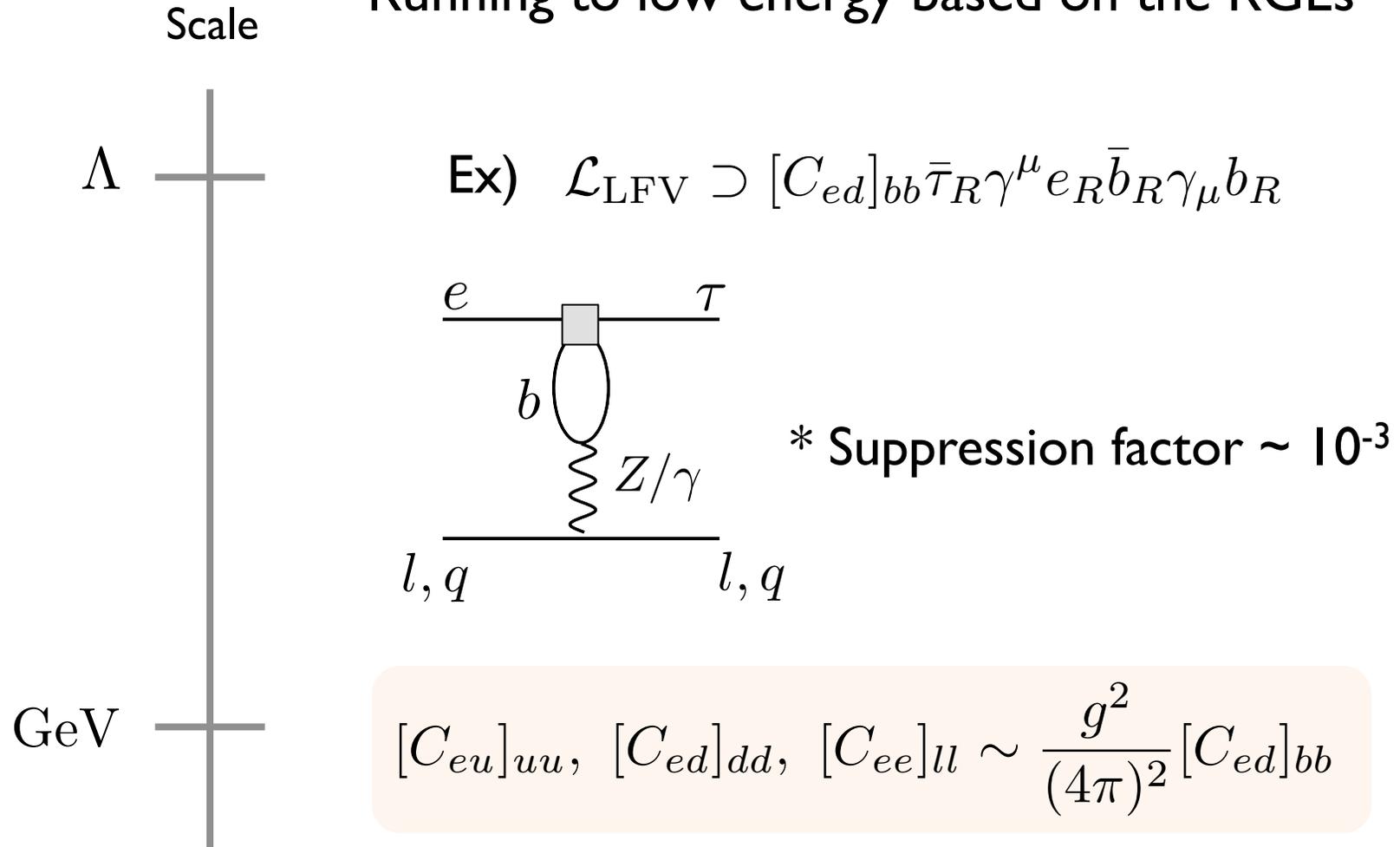
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$\tau \rightarrow e\mu^+\mu^-$	2.7×10^{-8}
$\tau \rightarrow ee^+e^-$	2.7×10^{-8}
$\tau \rightarrow e\eta$	1.6×10^{-8}

What about heavy-quark operators?

Scale running effects based on the RGEs

Scale running effects

Running to low energy based on the RGEs



Can be constrained by low-energy tau decays!

- Z decay $\text{BR}(Z \rightarrow \tau e) < 8.1 \times 10^{-6}$ (95% C.L.)

OPAL collaboration, Phys. C 67 (1995) 555{564}.

- Higgs decay $\text{BR}(H \rightarrow e^- \tau^+ + \tau^- e^+) < 4.7 \times 10^{-3}$ (95% C.L.)

ATLAS collaboration, PLB 800 (2020) 135069

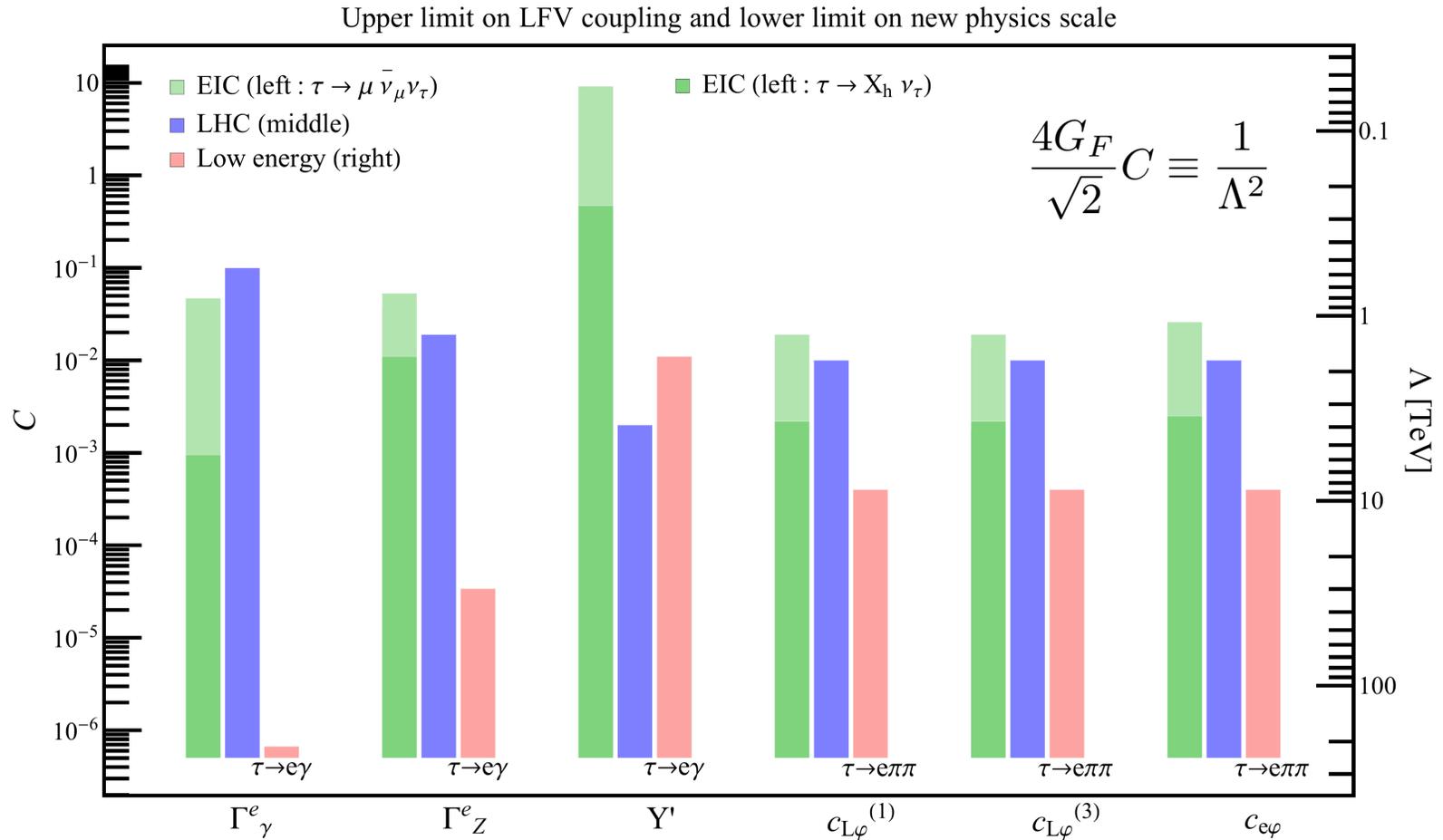
- Top decay $\text{BR}(t \rightarrow q l l') < 1.86 \times 10^{-5}$ (95% C.L.)

ATLAS collaboration, ATLAS-CONF-2018-044

- ATLAS Search $pp \rightarrow \tau e$ PRD98(2018)092008, [1807.06573]
Eur. Phys. J. C 76 (2016) 541, [1607.08079].

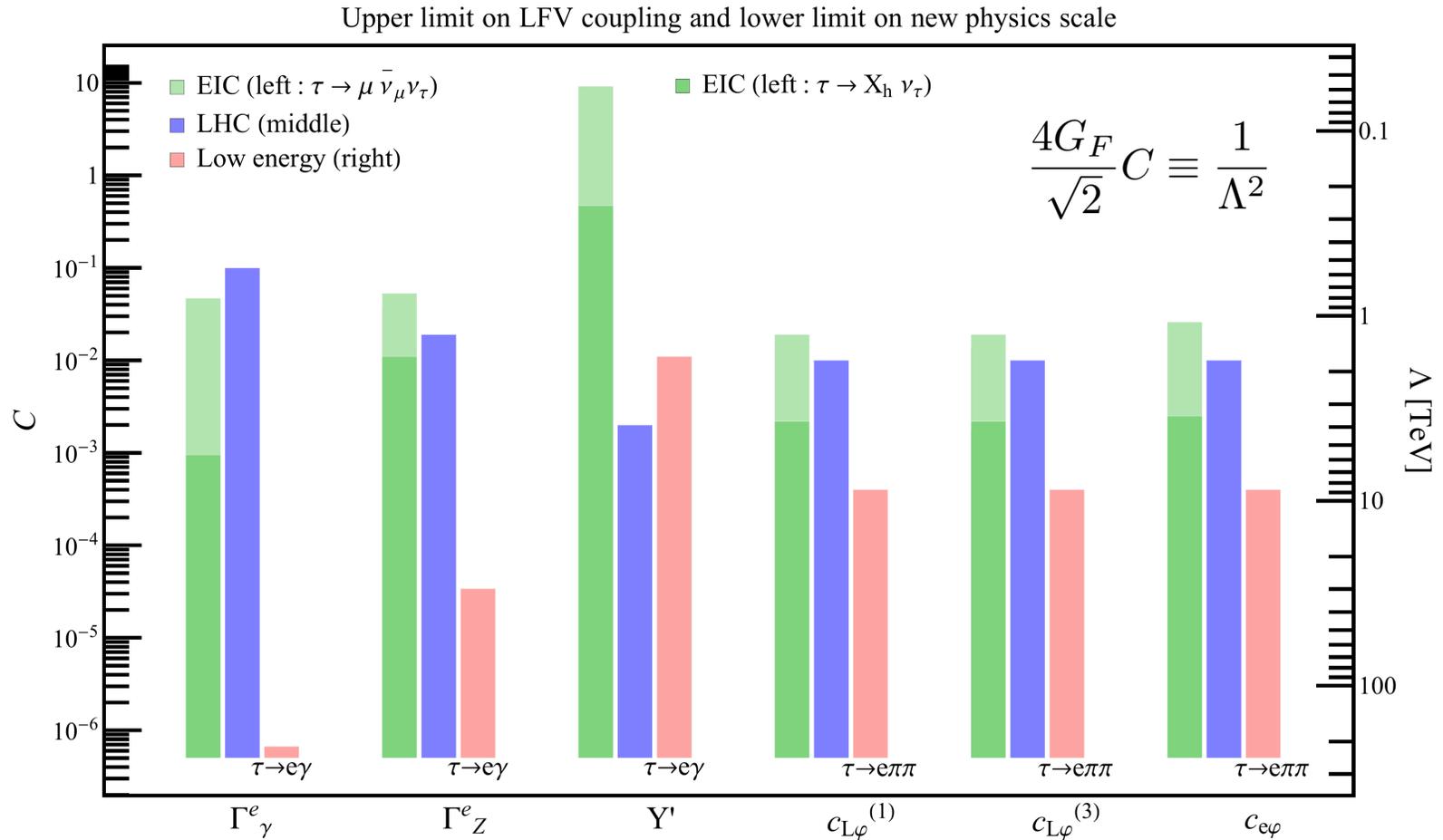
✓ Bound up-type flavor-violating operators

Dipole operator



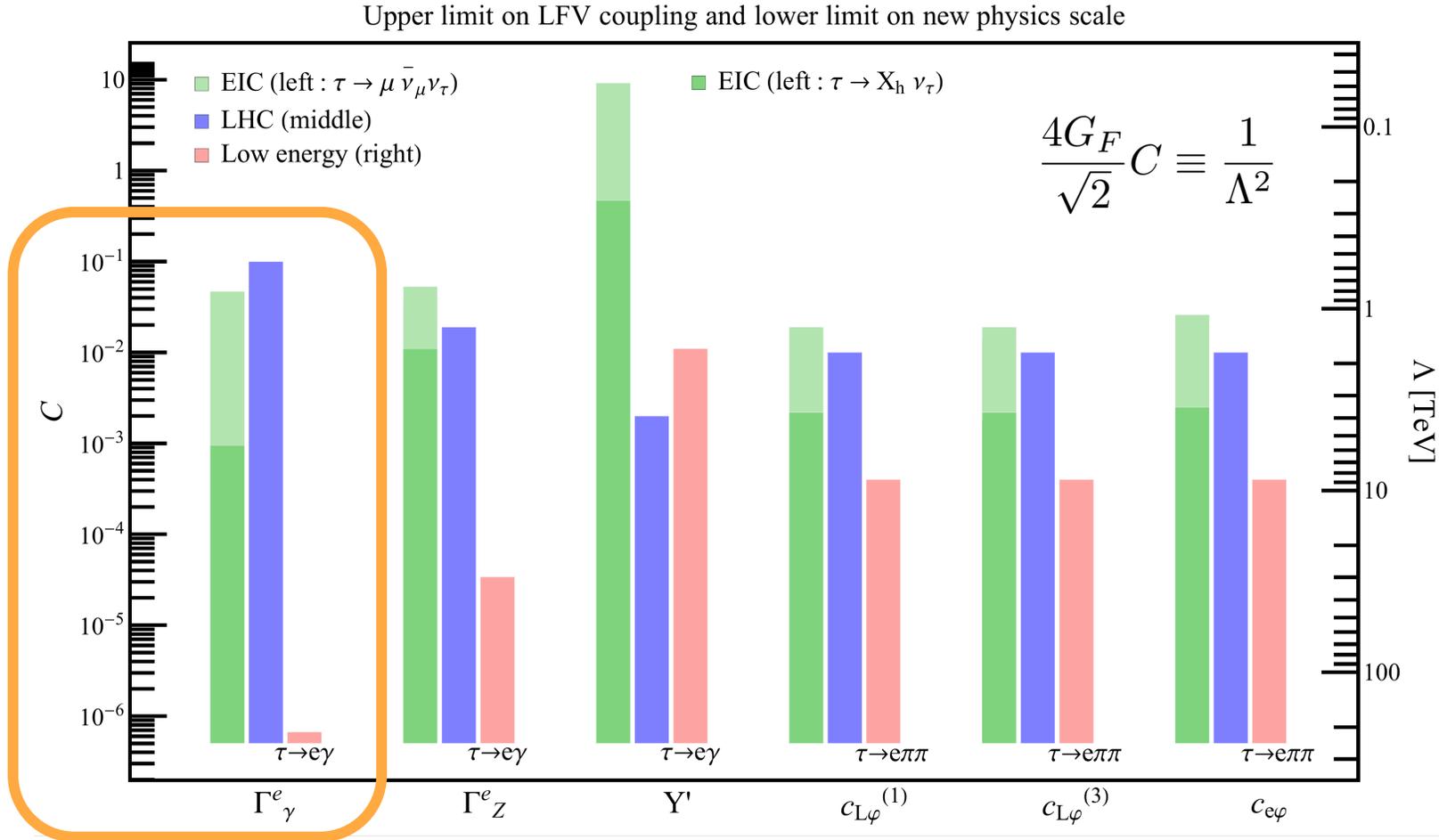
Leftmost (Rightmost) axis : Limit on operator (Λ)

Dipole operator



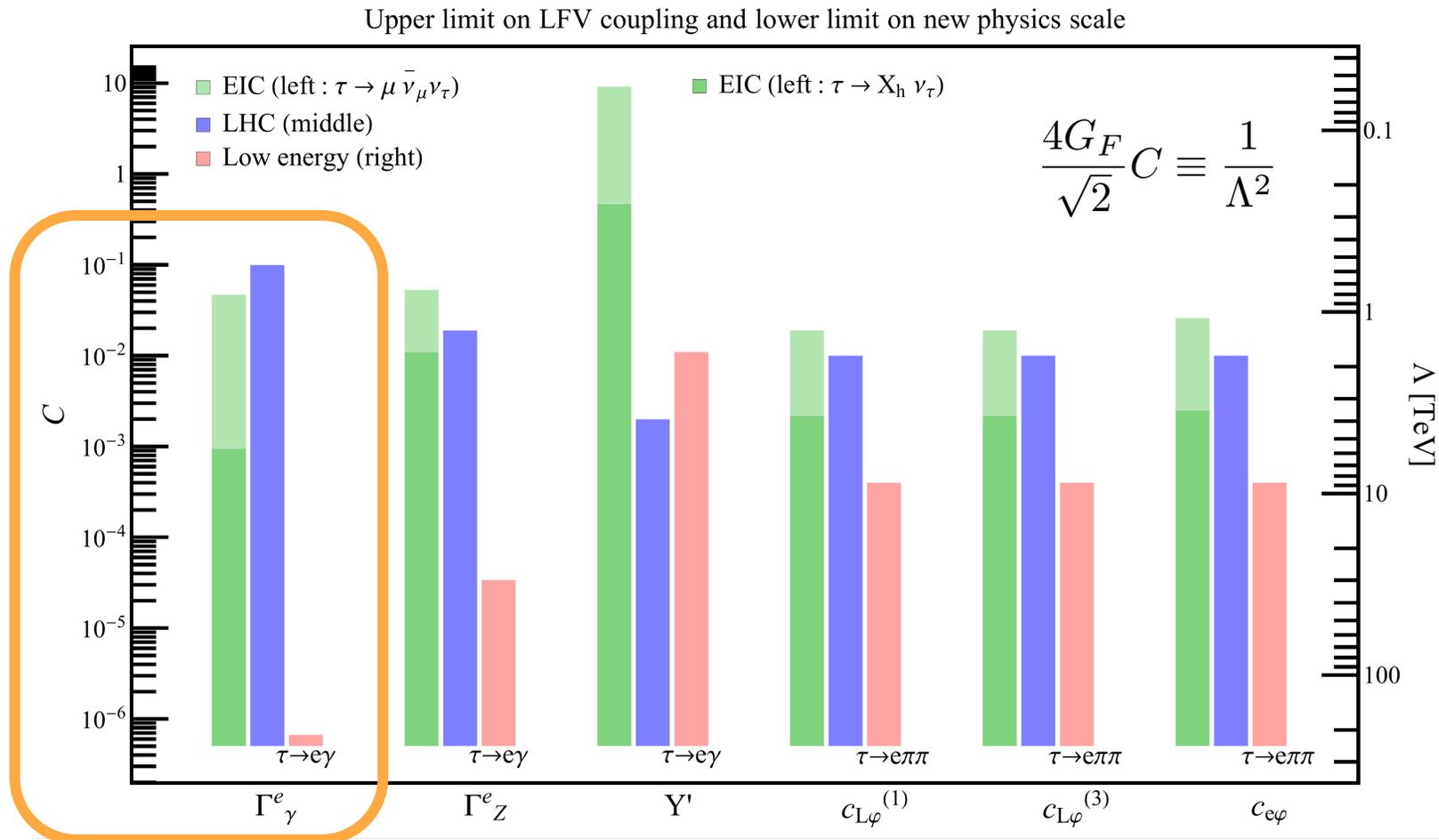
■ EIC ($\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau$)
 ■ LHC
 ■ Tau decays

Dipole operator

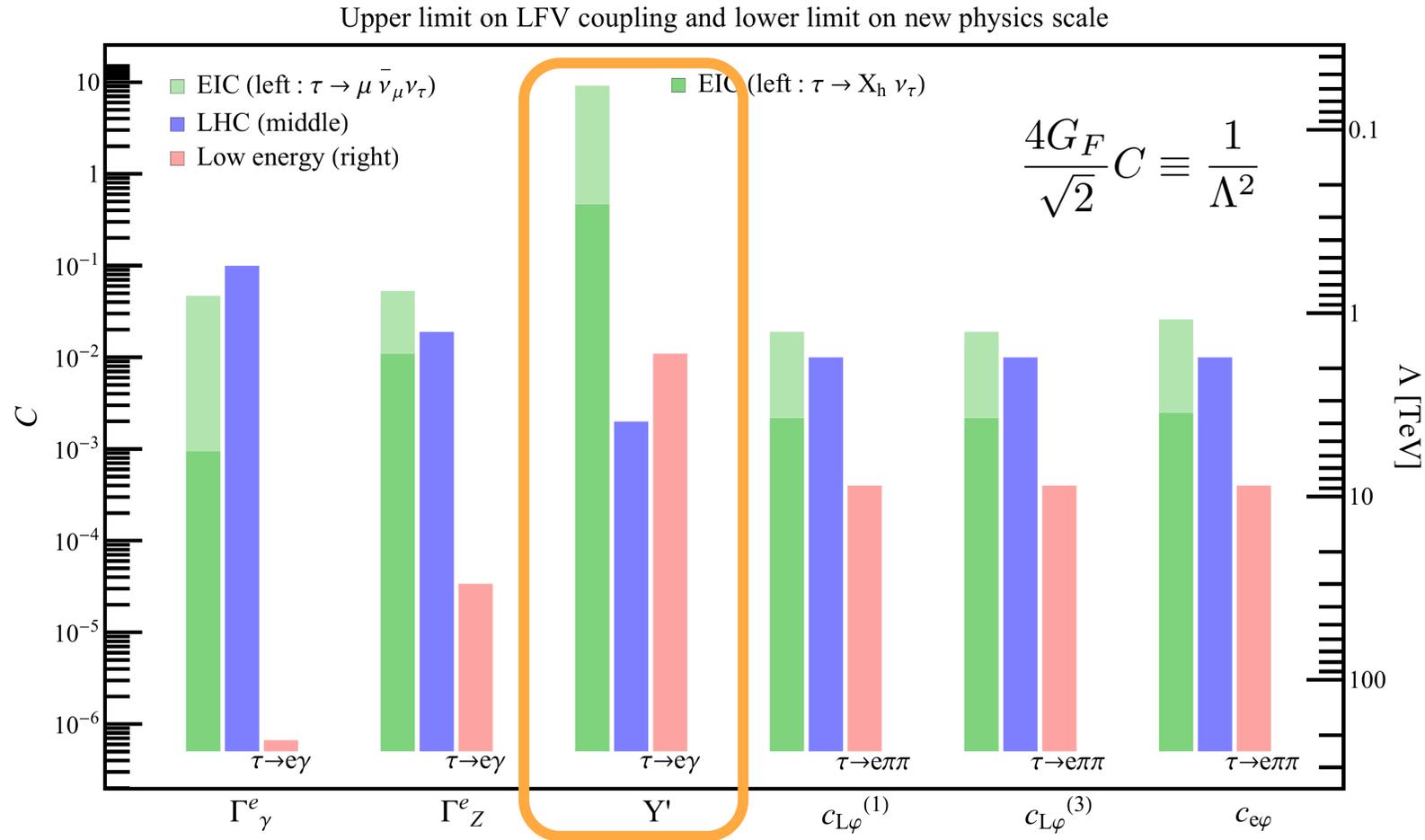


EIC, LHC : $\Gamma_\gamma^e \lesssim 0.1$ Tau e gamma : $\Gamma_\gamma^e < 6.7 \times 10^{-7}$

Dipole operator



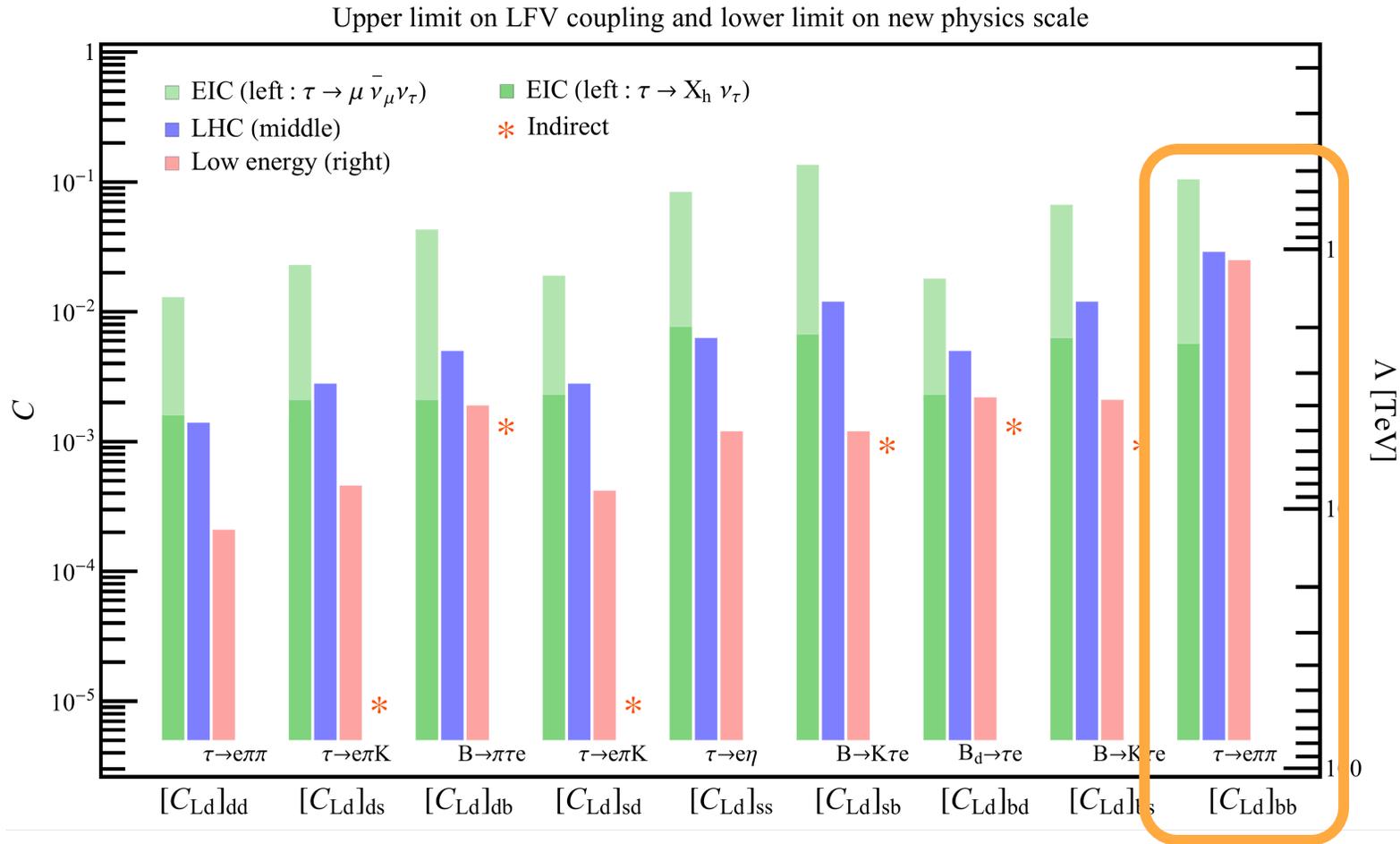
EIC, LHC : $\Gamma_\gamma^e \lesssim 0.1$ Tau e gamma : $\Lambda \gtrsim 200$ TeV



LHC : $[Y'_e]_{\tau e} < 2 \times 10^{-3}$

Tau e gamma : $[Y'_e]_{\tau e} < 1.1 \times 10^{-2}$

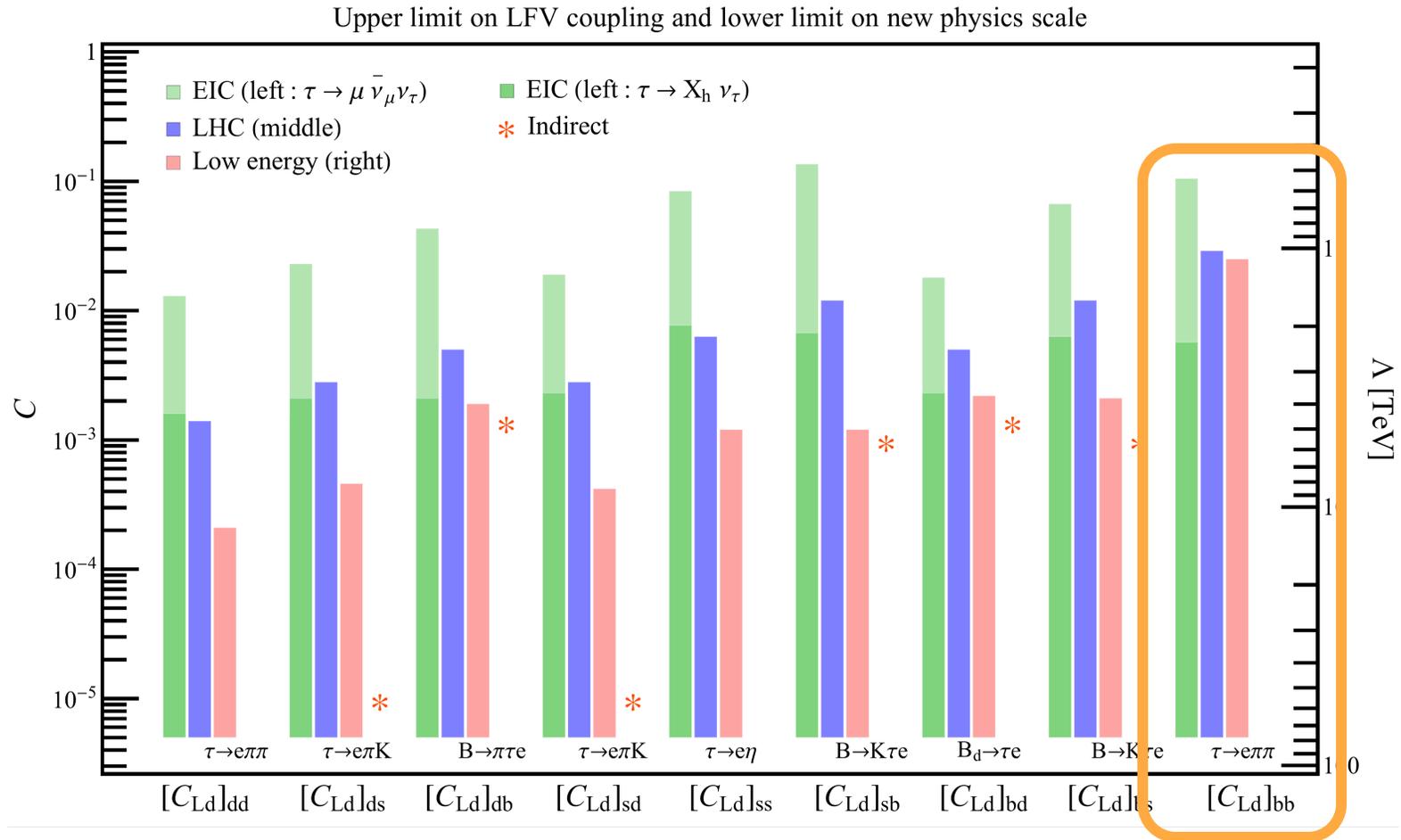
VLR bottom



EIC : $[C_{Ld}]_{bb} < 0.1$

LHC, Tau decay : $[C_{Ld}]_{bb} < O(10^{-2})$

VLR bottom



Dark Green

EIC ($\tau \rightarrow X_h \nu_\tau$) $[C_{Ld}]_{bb} < 6.8 \times 10^{-3}$ ($\epsilon = 1$)

Multi-operator scenario

See the situation where 8 operators are nonzero

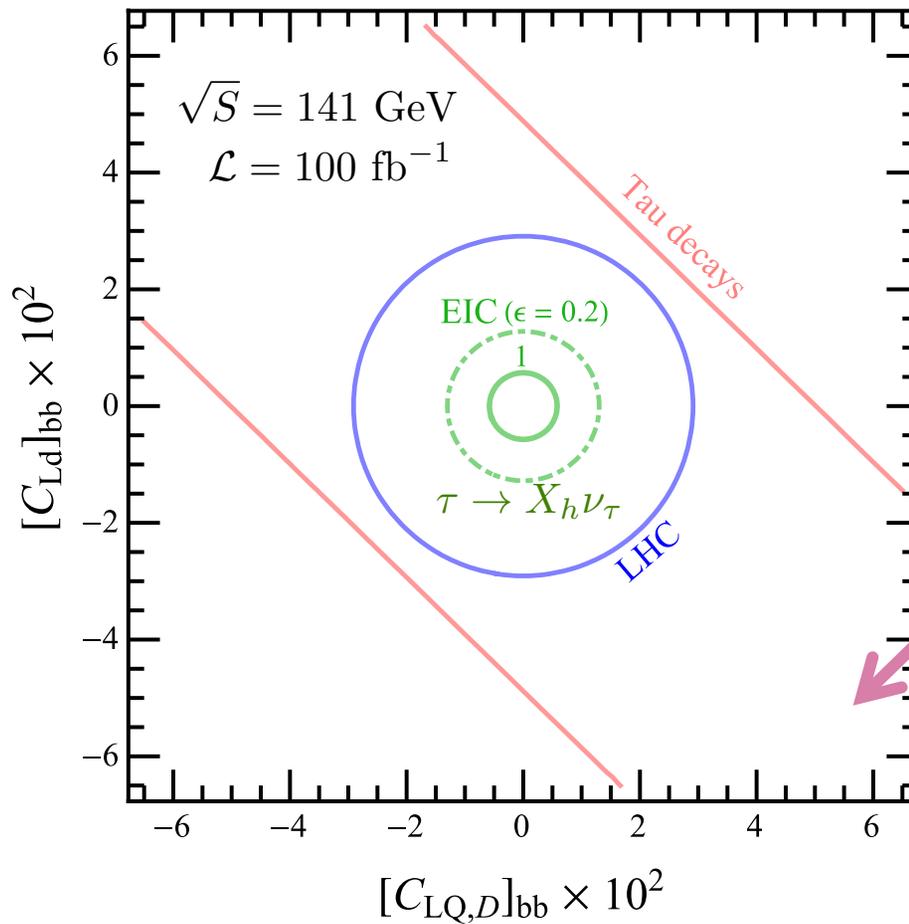
* Z couplings + down-type 4F operators

$$\begin{aligned} \mathcal{L}_{\text{LFV}} \supset & -\frac{g_2}{c_W} \left(c_{L\varphi}^{(1)} + c_{L\varphi}^{(3)} \right) \bar{\tau}_L \gamma^\mu Z_\mu e_L \\ & -\frac{4G_F}{\sqrt{2}} \sum_{a=d,s,b} [C_{Ld}]_{aa} \bar{\tau}_L \gamma^\mu e_L \bar{d}_{Ra} \gamma_\mu d_{Ra} \\ & -\frac{4G_F}{\sqrt{2}} \sum_{a=d,s,b} [C_{LQ,D}]_{aa} \bar{\tau}_L \gamma^\mu e_L \bar{d}_{La} \gamma_\mu d_{La} \end{aligned}$$

✓ Limits on $[C_{LQ,D}]_{bb}$ and $[C_{Ld}]_{bb}$ at 90% C.L.

The rest is marginalized.

Multi-operator scenario



Free direction appears.

$$[C_{LQ,D}]_{bb} - [C_{Ld}]_{bb}$$



Collider probes are necessary to close the free direction.

Summary

The discovery of neutrino oscillation implies nonzero neutrino mass.



Key approach : Fundamental symmetry tests

Ex) Lepton number / flavor violation

*Search for neutrinoless double beta decay is a probe of **Majorana mass**.*

Our study : Model-independent analyses with light V_R

Possible to analyze NDBD in any mass spectrum
with interpolation formulae

✓ *Intensity frontier to unravel the neutrino nature will be more advanced.*